

**What have we learnt about the ocean  
and climate using adjoint models  
that we perhaps did not know  
before?**

**Andy Moore  
Ocean Sciences Dept  
University of California Santa Cruz**

**What have we learnt about the ocean  
and climate using adjoint models  
that we perhaps did not appreciate  
before?**

**Andy Moore  
Ocean Sciences Dept  
University of California Santa Cruz**

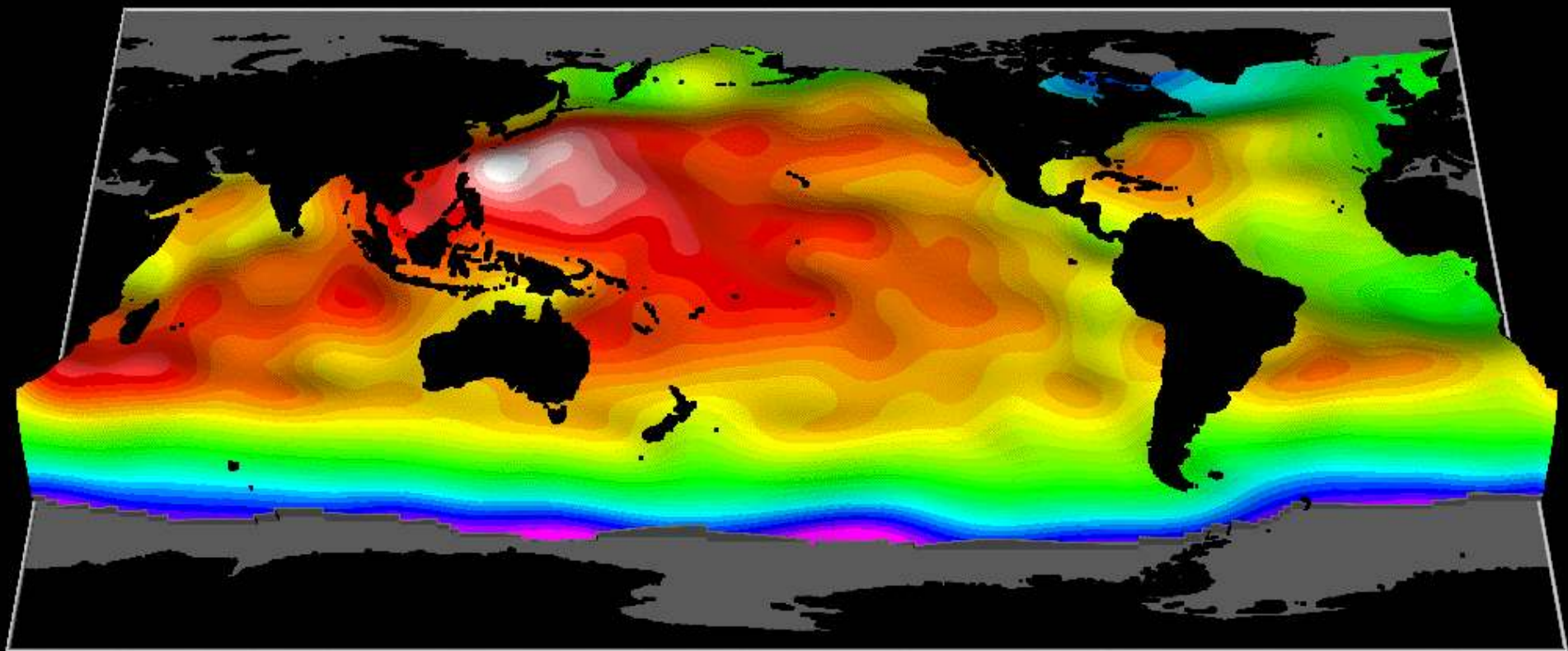
An exercise in hindsight...

# Increasing Scales

- Island wakes and passages
- Coastal currents and upwelling
- Linear waves and ocean gyres
- Thermohaline circulation
- Tropical climate variability

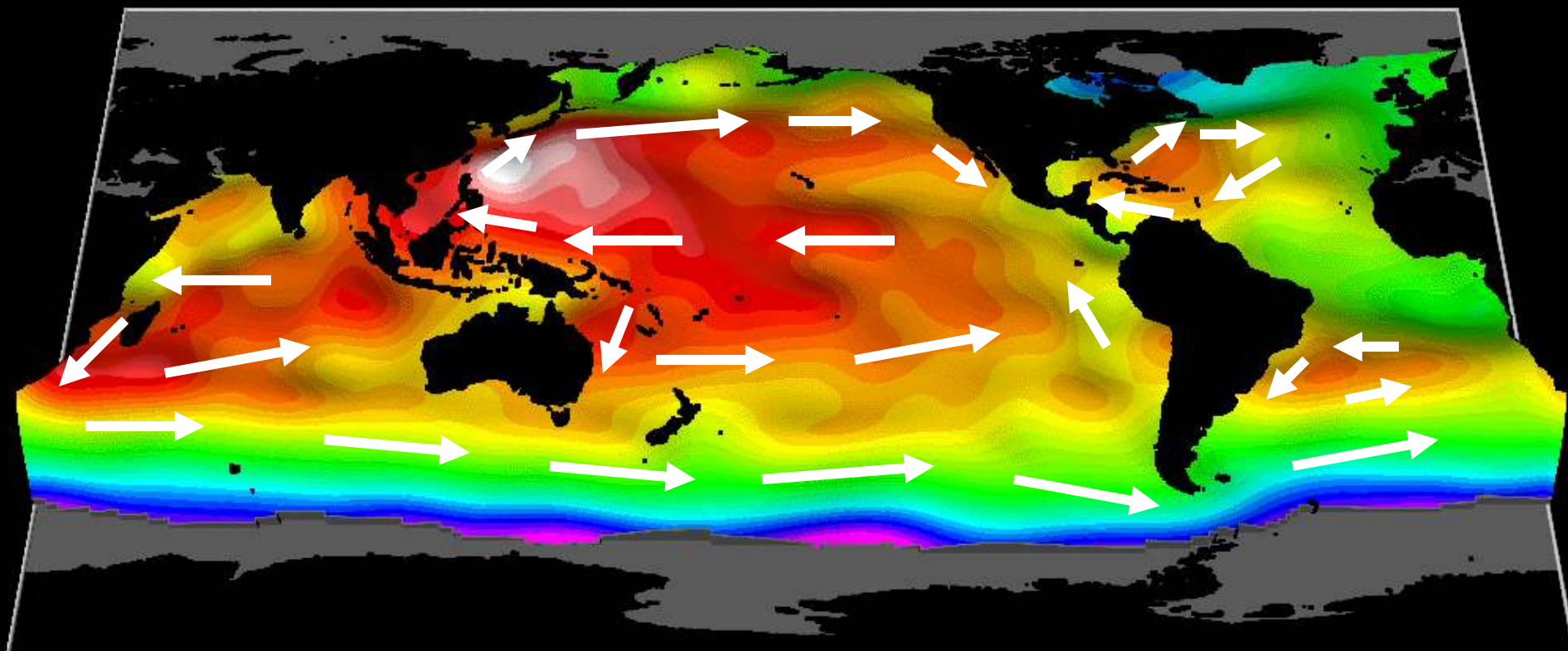
# Tools of the Trade

- Adjoint sensitivity analysis
- Singular value decomposition
- Data Assimilation



■ No Valid Data

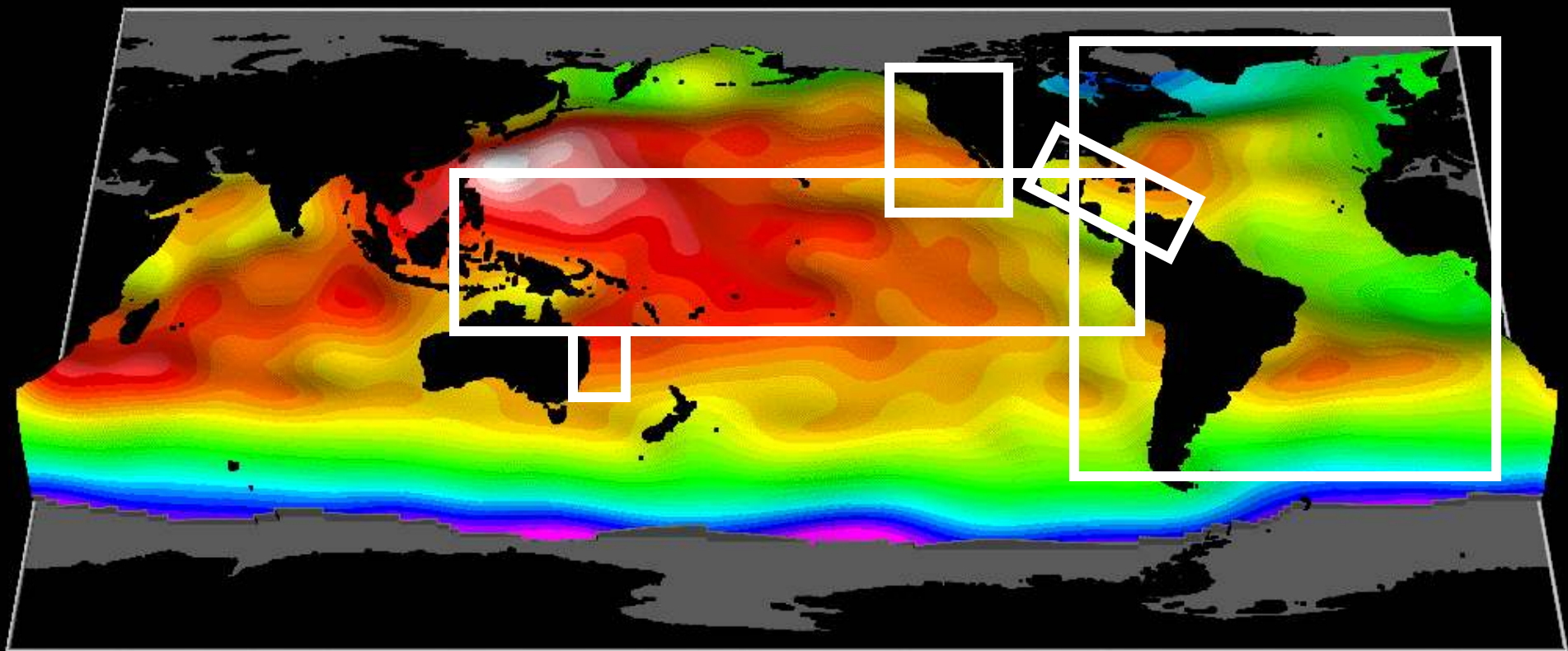
Ocean Dynamic Topography (cm) Oct 3-12, 1992



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

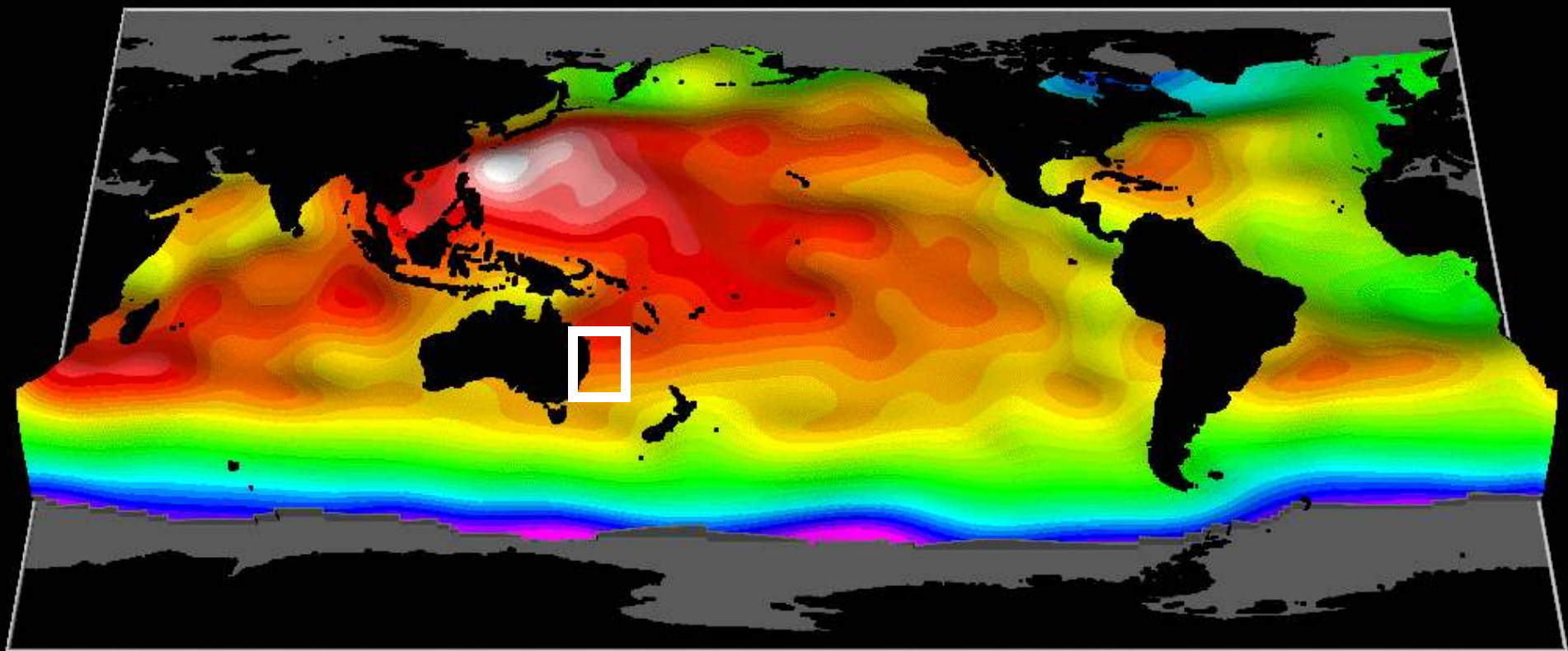




■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992





■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992



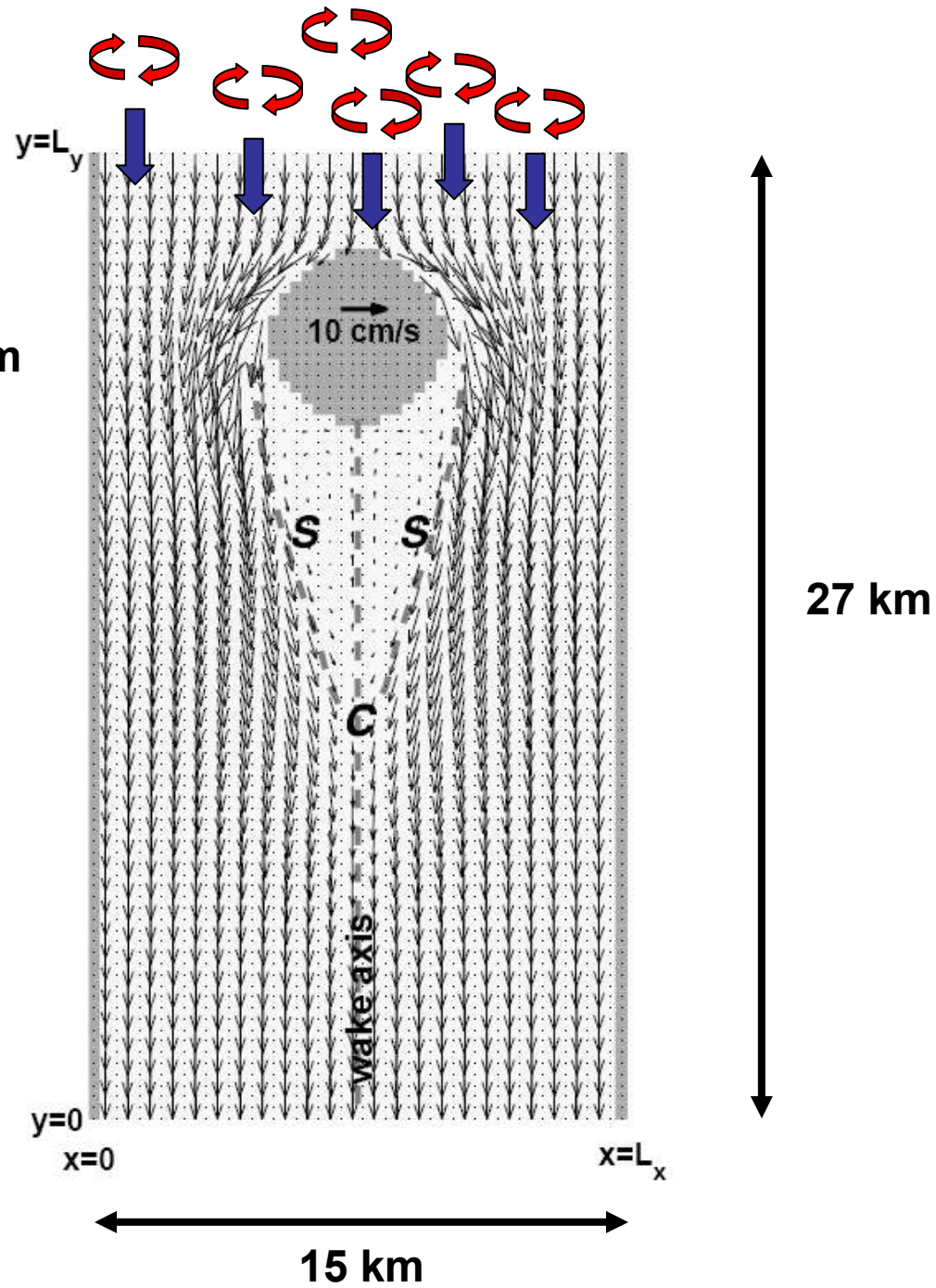






Island radius= 5 km  
Channel depth = 10 m

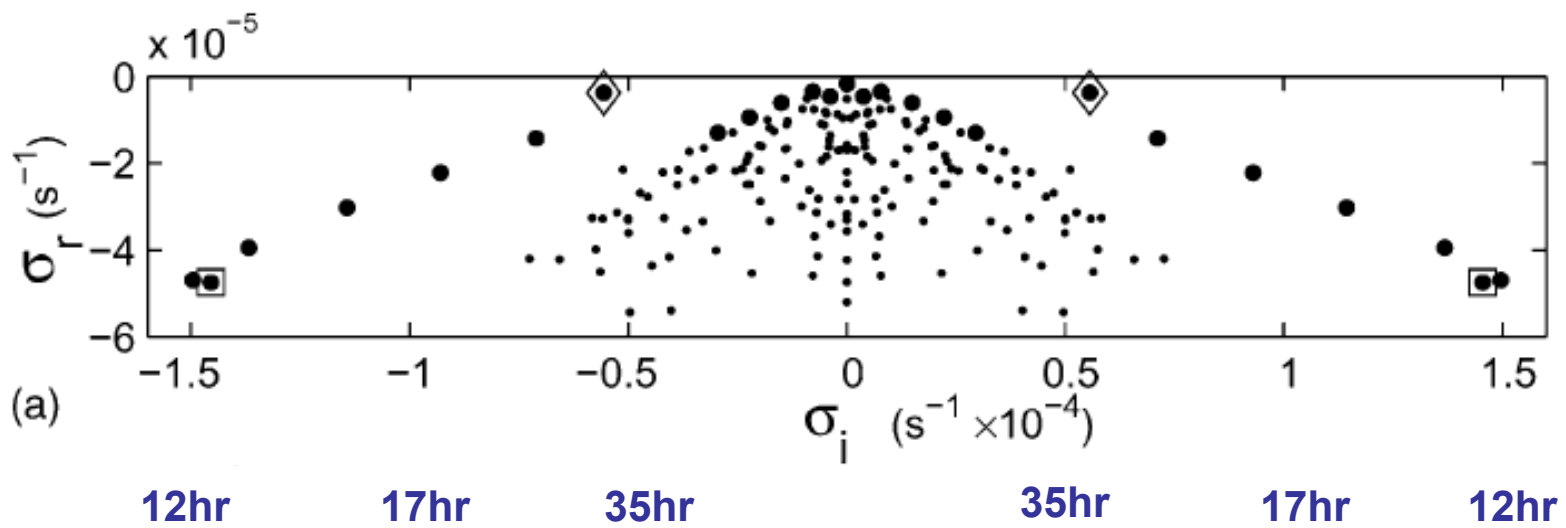
Aiken et al (2003)



# Tools Used & Relevant Ideas

- Singular value decomposition of stochastically-forced circulation variance
- “Stochastic optimals”
- Pseudospectra
- Nonnormal dynamics: linear eigenmode interference
- Model: barotropic, shallow water.

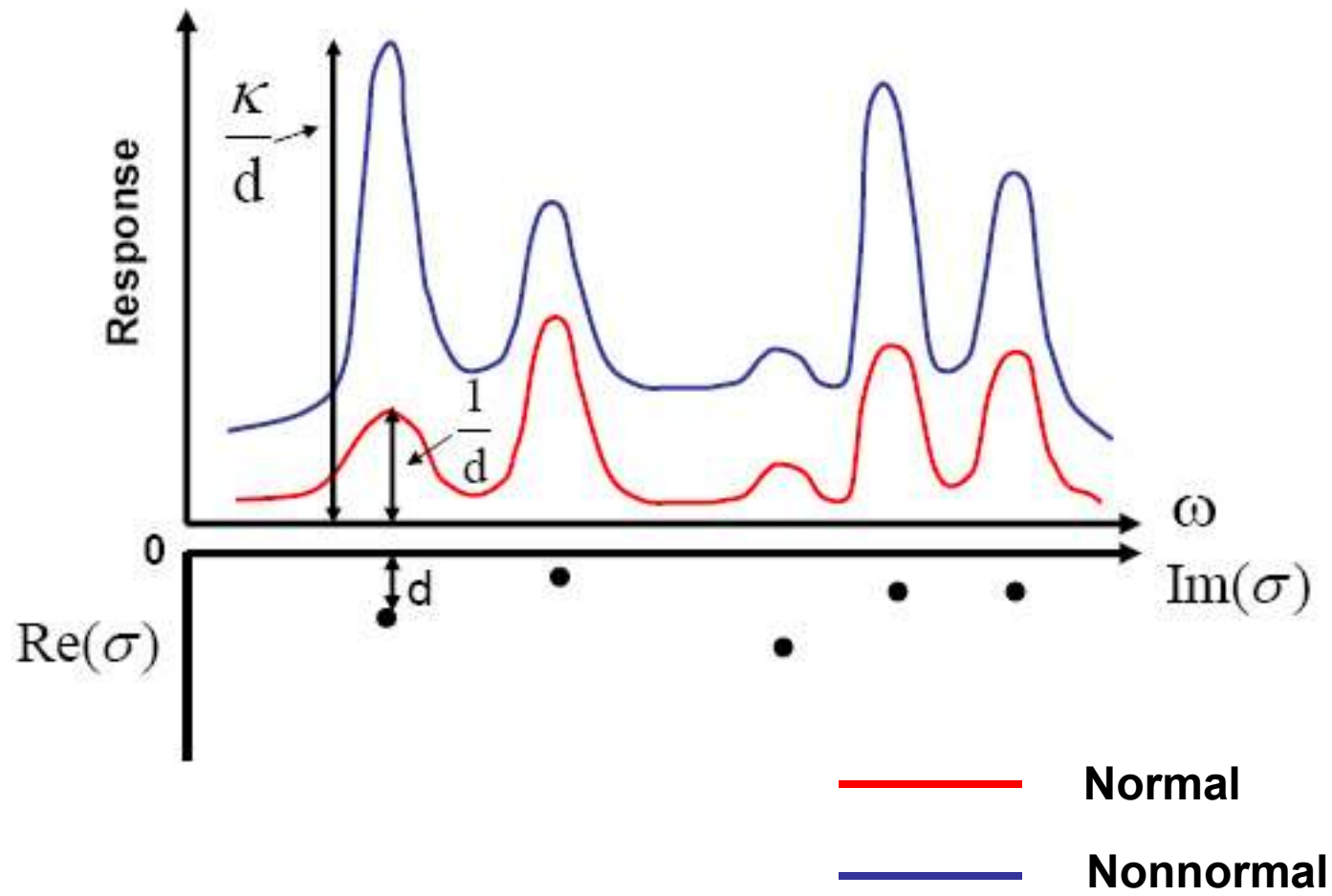
# Eigenspectrum



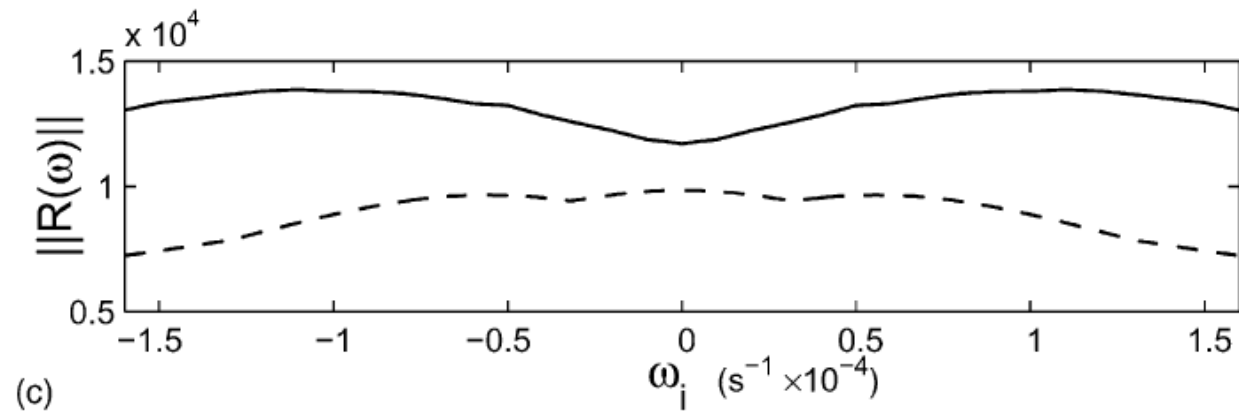
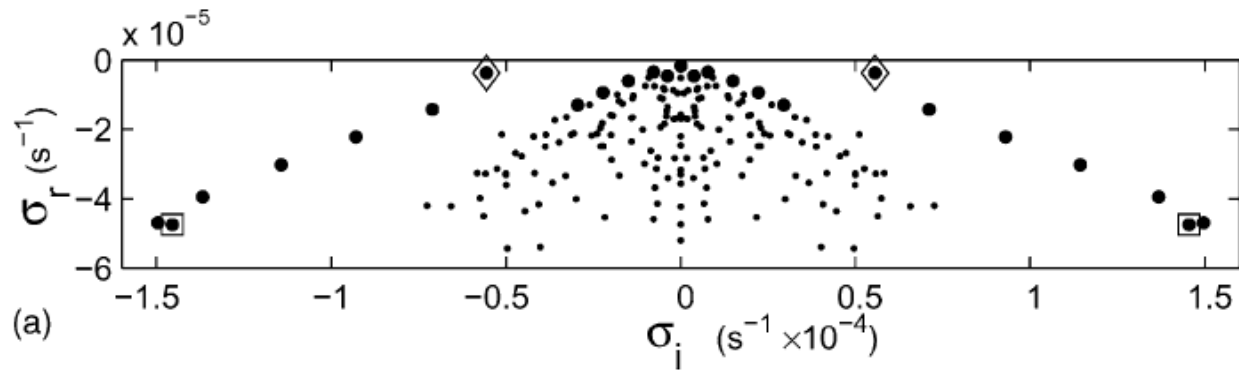
**Subcritical Reynolds number**



# Resonance vs Pseudoresonance



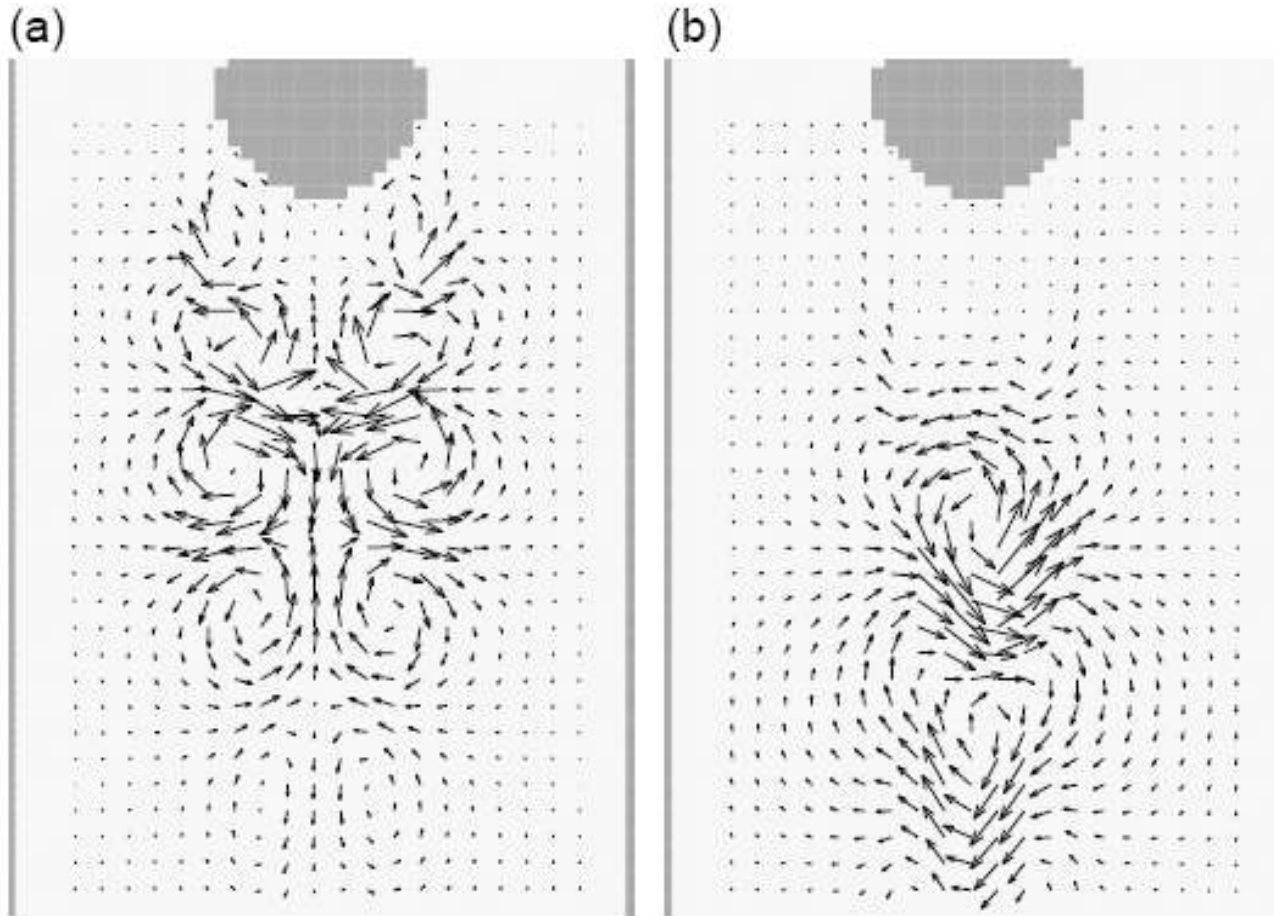
# Pseudoresonance



----- Normal  
————— Nonnormal

# Pseudoresonance

Leading EOF in presence of stochastic forcing



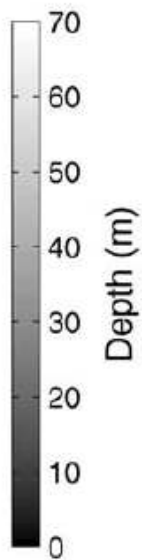
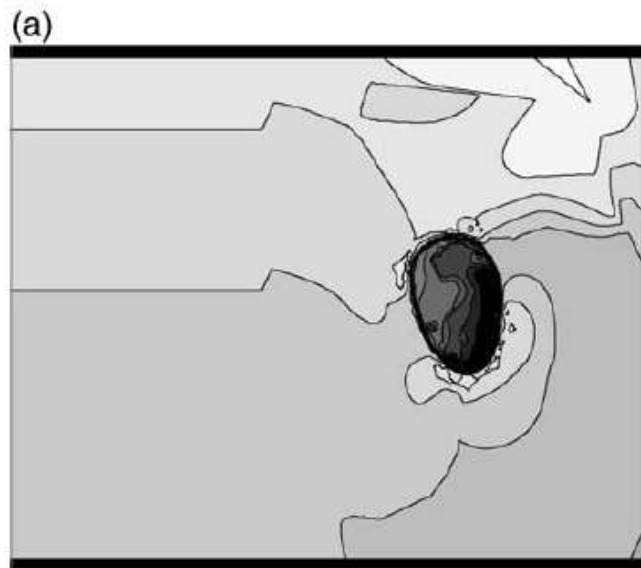
**Symmetric  
forcing**

**Asymmetric  
forcing**

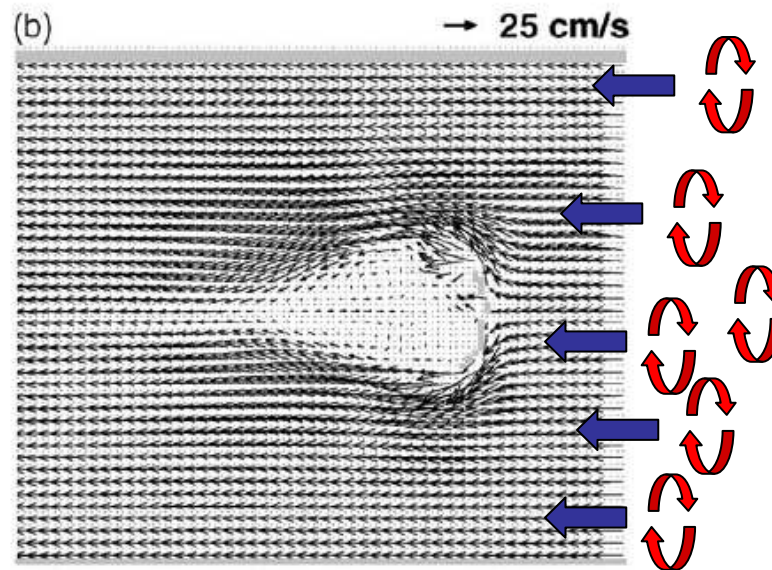


**Bowden  
Reef**

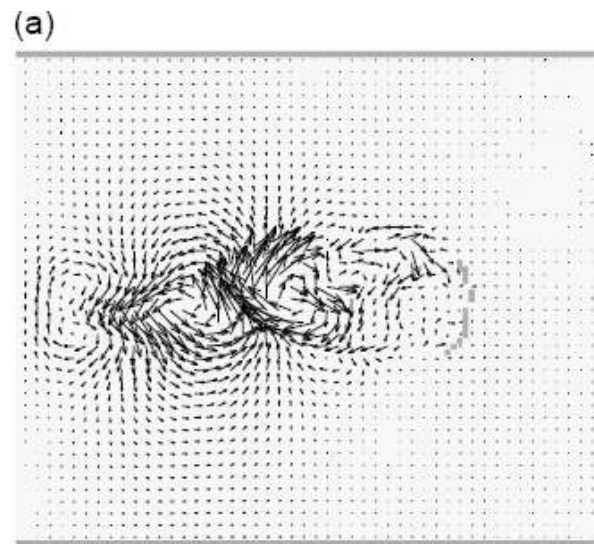




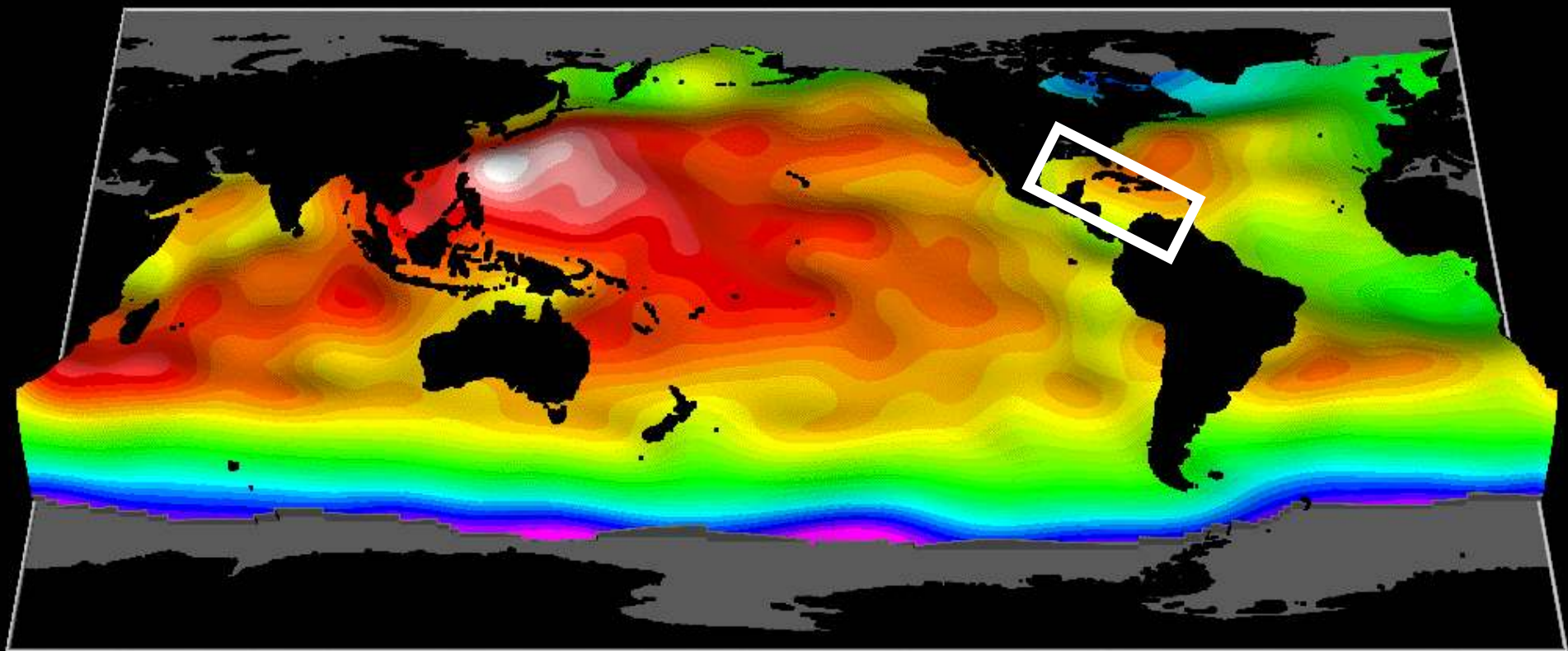
## Steady incident flow



## Bowden Reef



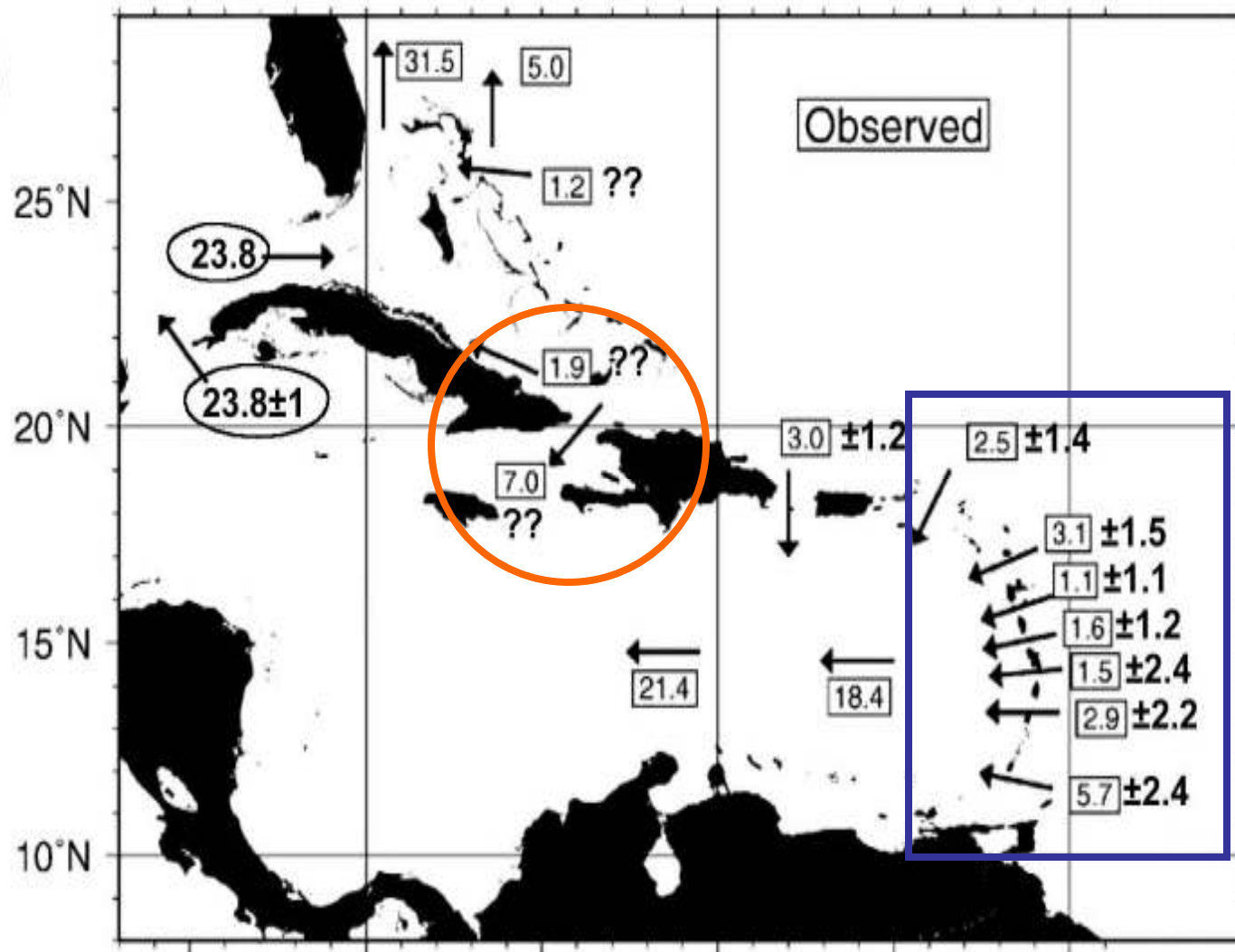
## Leading EOF with stochastic forcing



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

# Island Passage Transport Variability



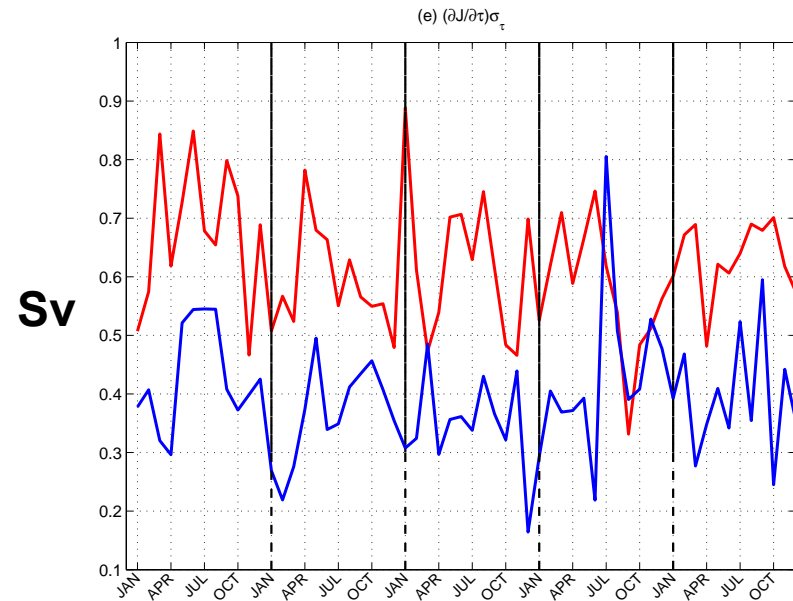
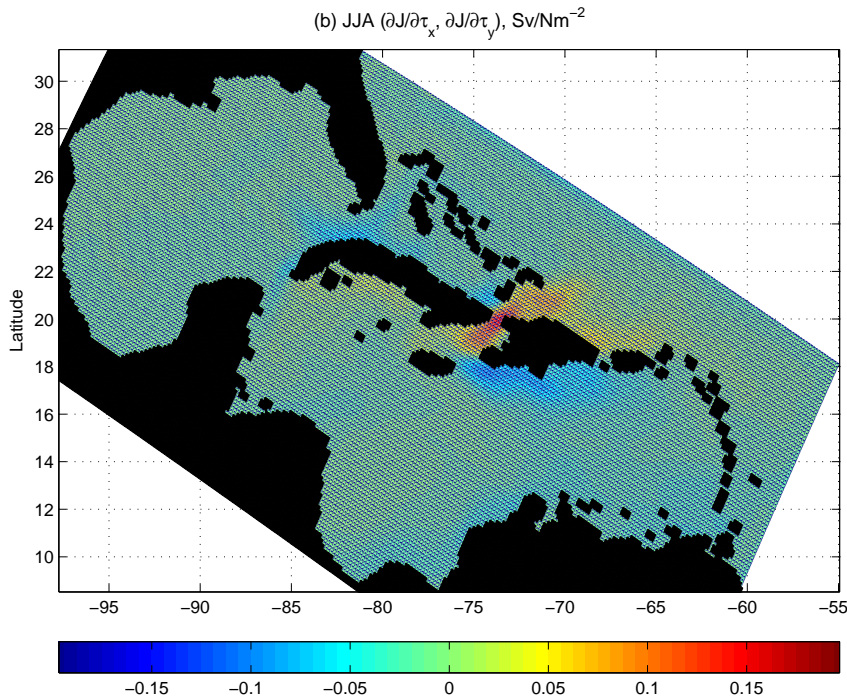
Wilson and Johns (1996)

$$1 \text{ Sv} = 10^6 \text{ m}^3 \text{ s}^{-1}$$



# Tools Used

- Adjoint sensitivity analysis
- Model: Regional Ocean Modeling System (ROMS)

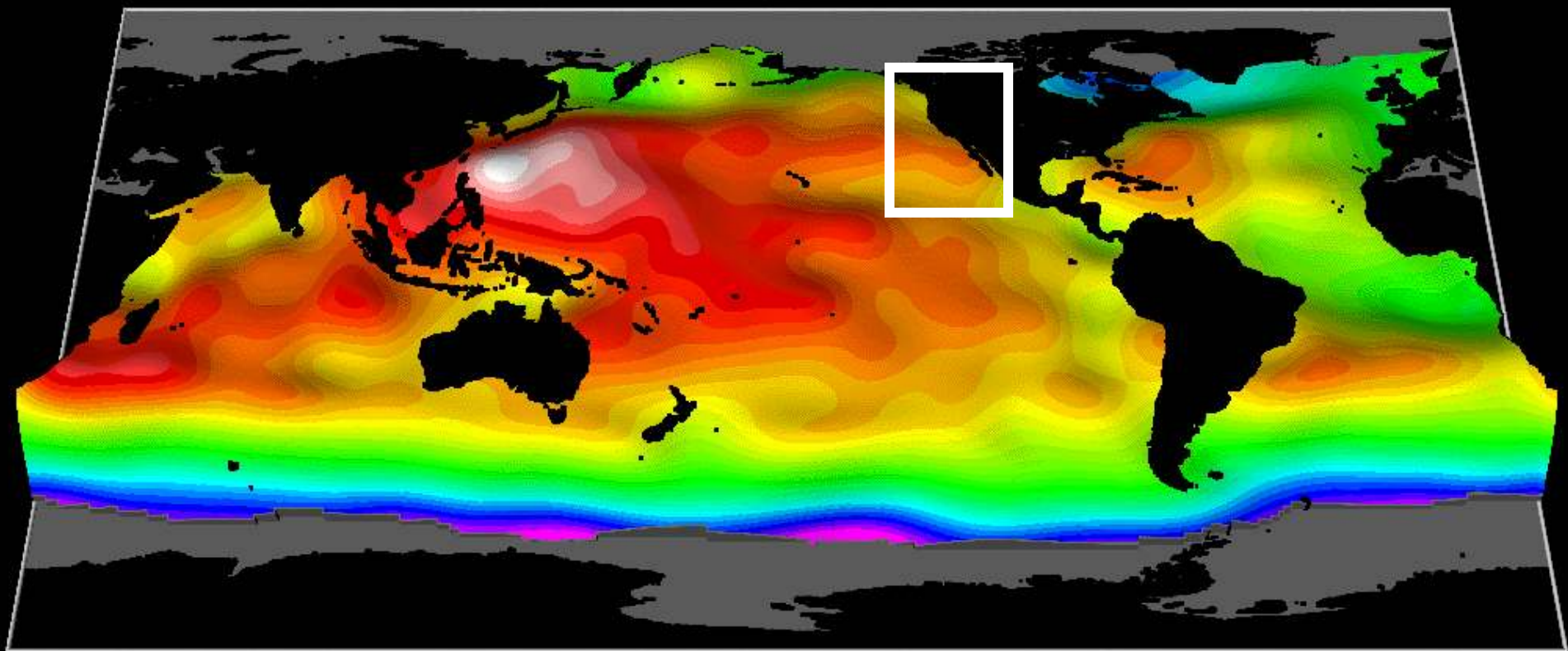


# Windward Passage Transport (Chhak, 2006)

**Transport driven by wind  
variability and via  
coastally trapped waves**

**— Zonal wind**  
**— Meridional wind**

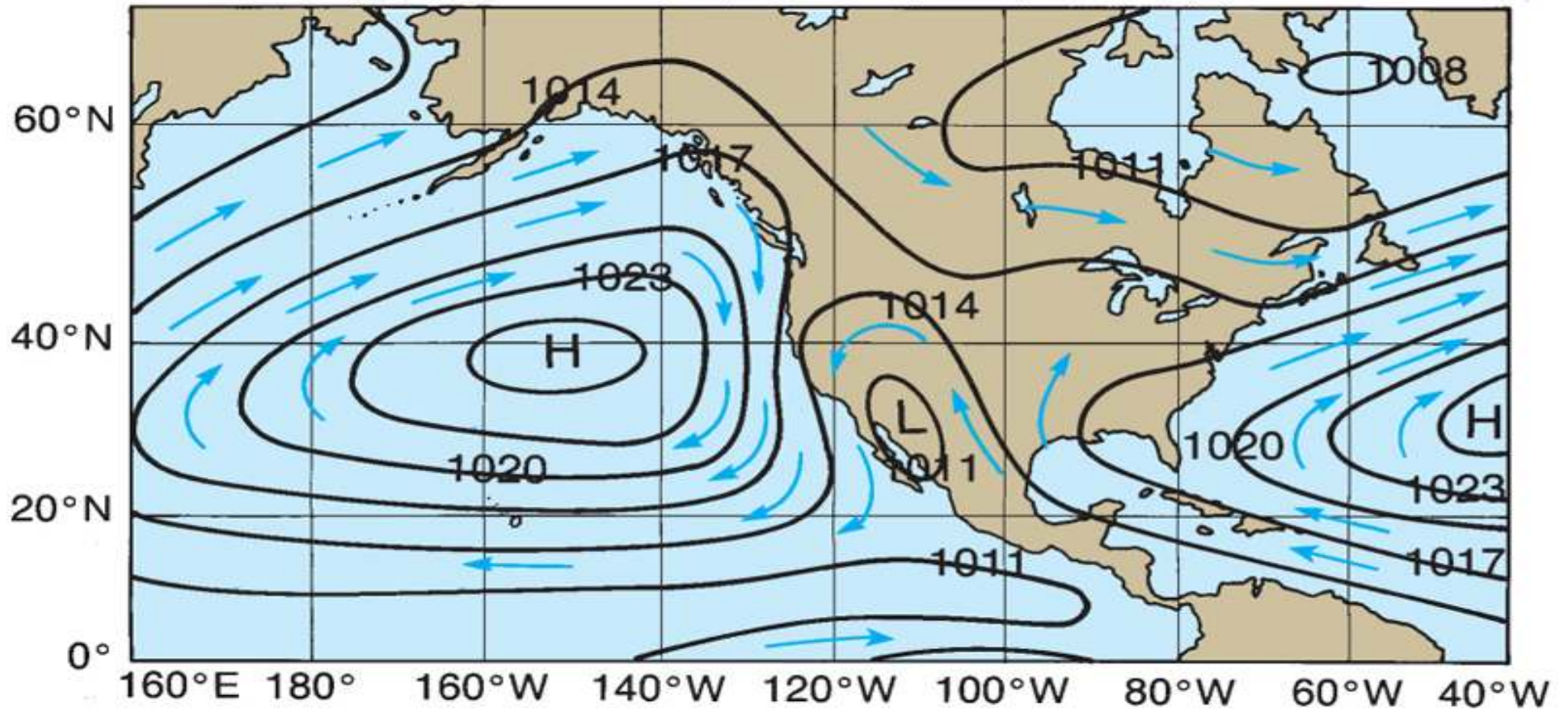
$$1 \text{ Sv} = 10^6 \text{ m}^3 \text{ s}^{-1}$$



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

# The California Current (CCS)



**Decadal variations in California Current  
Upwelling Cells  
(Chhak & Di Lorenzo, 2007)**

Tools used :

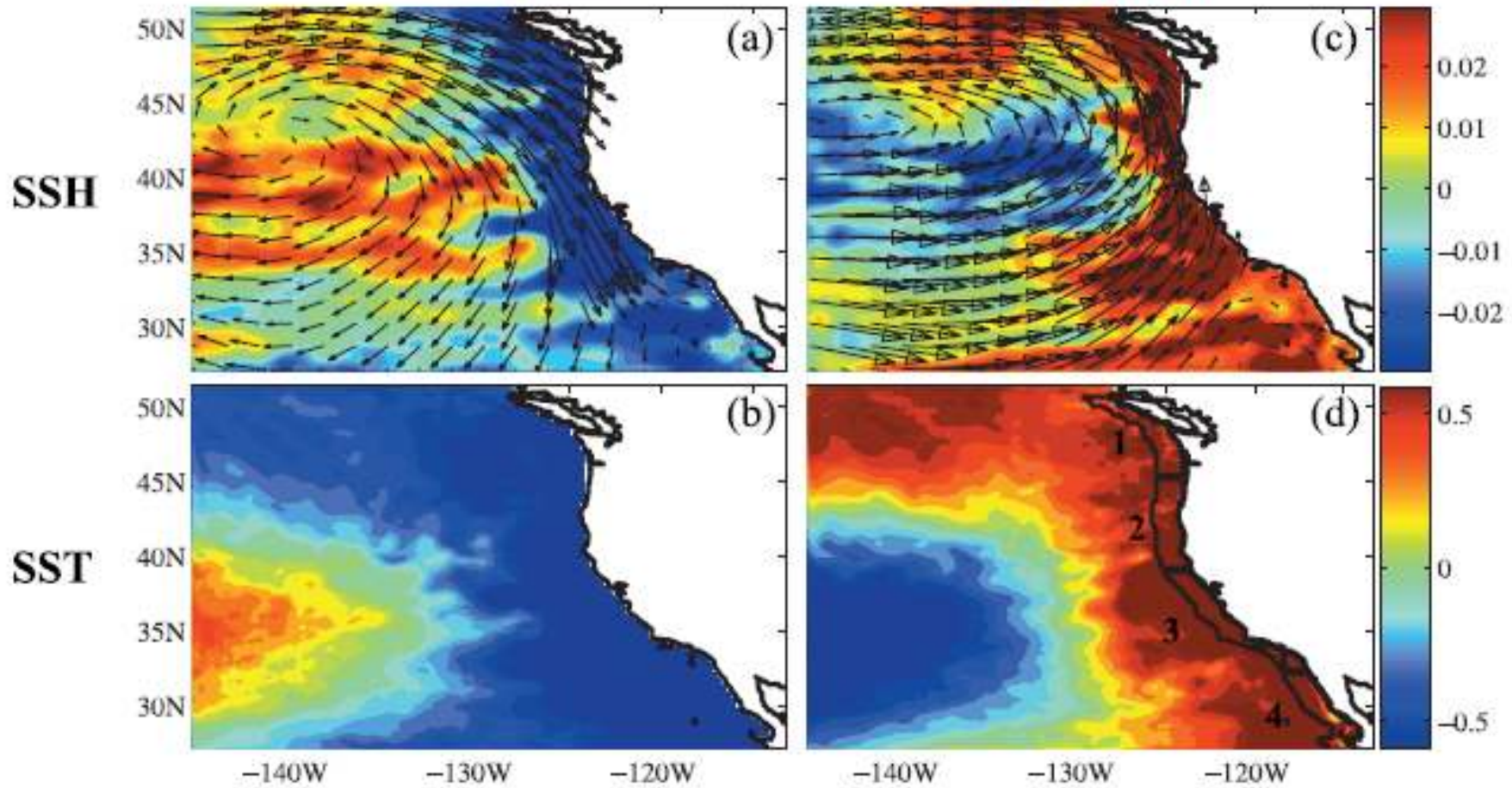
- Adjoint sensitivity analysis
- Model: Regional Ocean Modeling System (ROMS)



# Decadal variations in California Current Upwelling Cells (Chhak & Di Lorenzo, 2007)

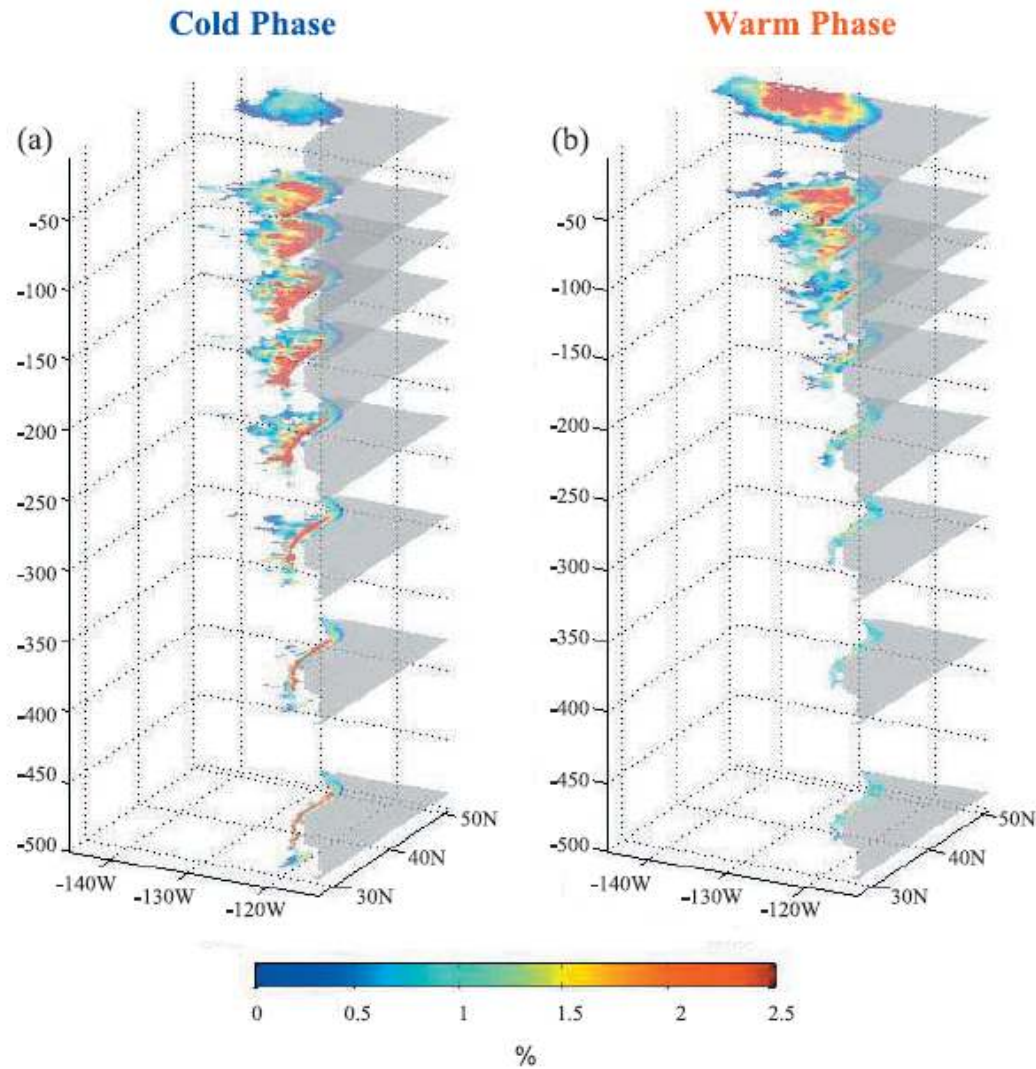
Cold Phase

Warm Phase



Pacific Decadal Oscillation (PDO)

Passive tracer introduced mid-April each year (55 yrs); adjoint run for 1 yr



Cold phase: deeper source of upwelled, nutrient rich water.

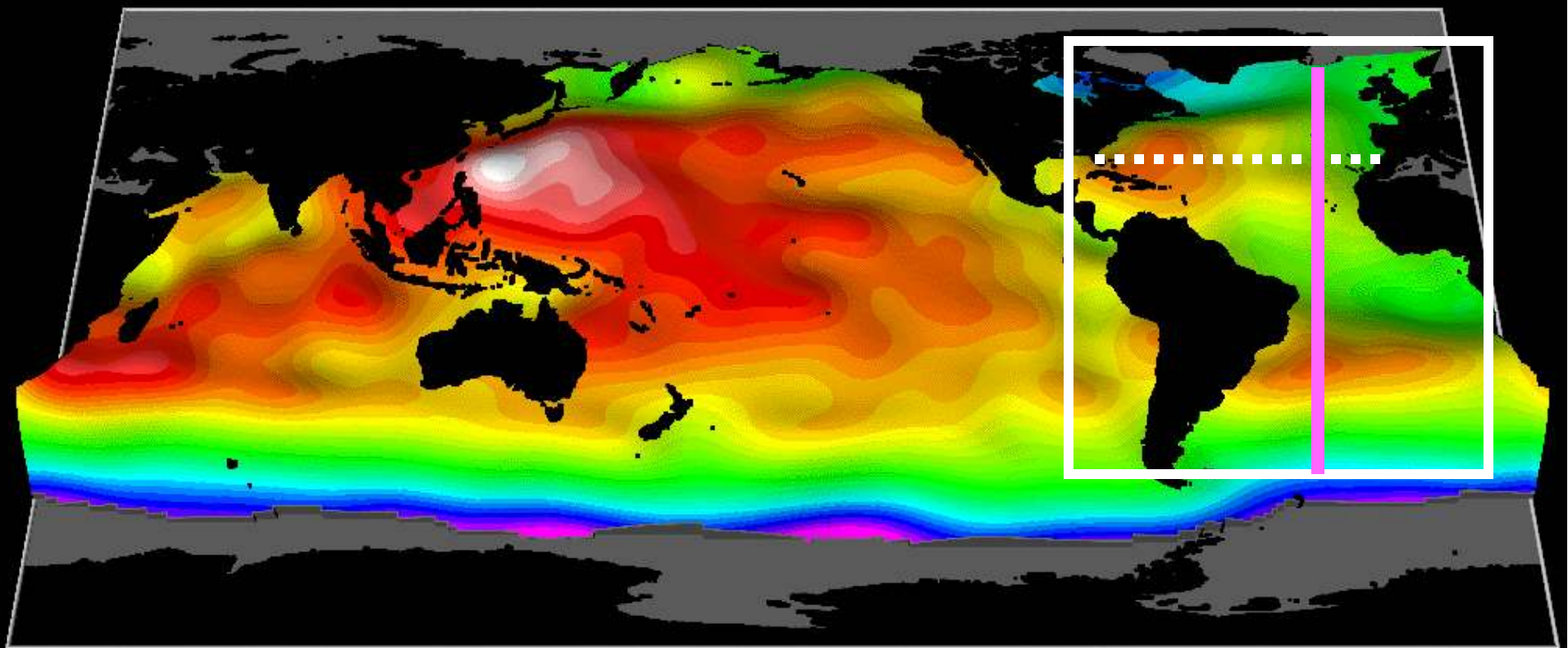


Supported by observations of phytoplankton & zooplankton

Origin of upwelling waters 1 yr prior to following year upwelling max.

Chhak & Di Lorenzo (2007)

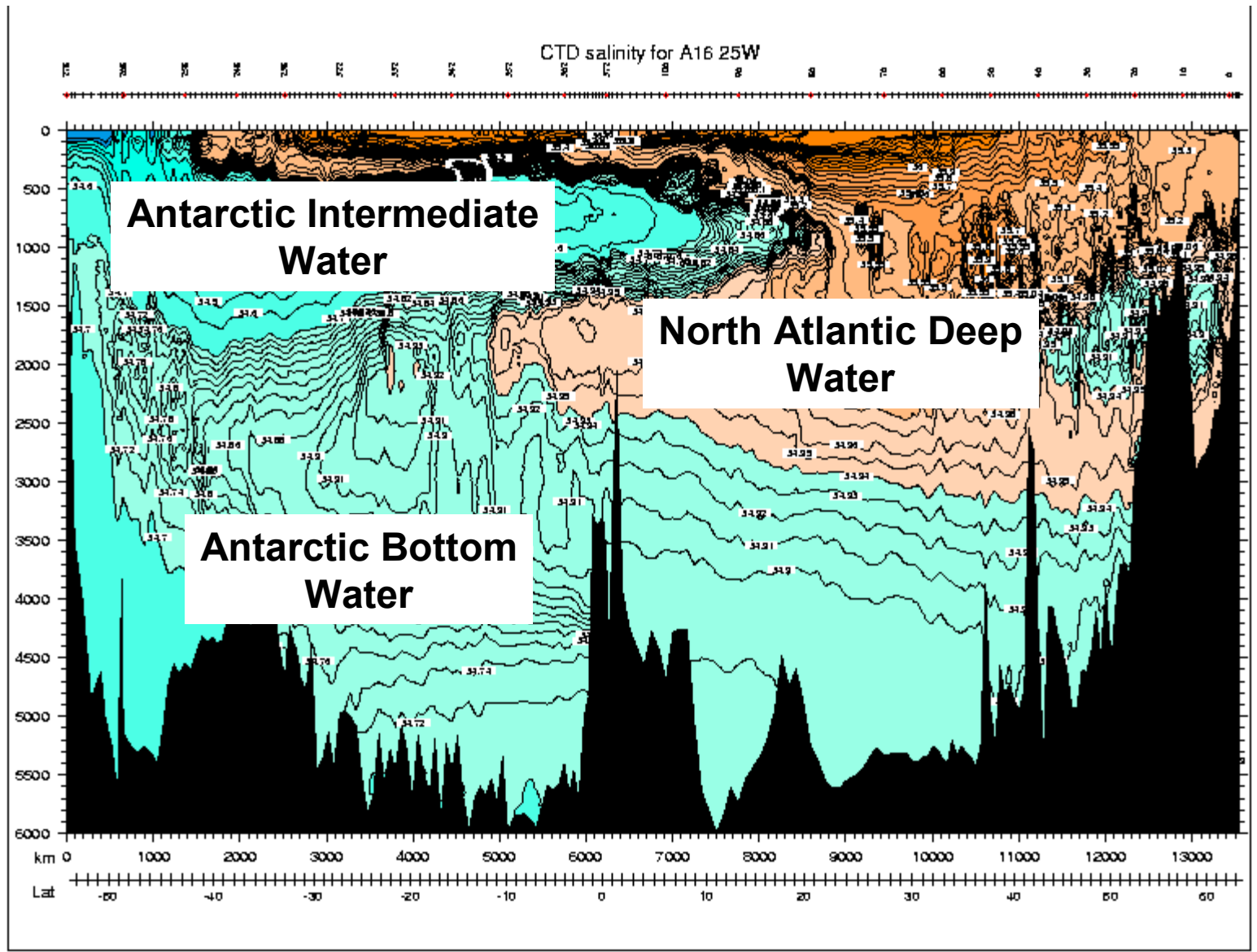




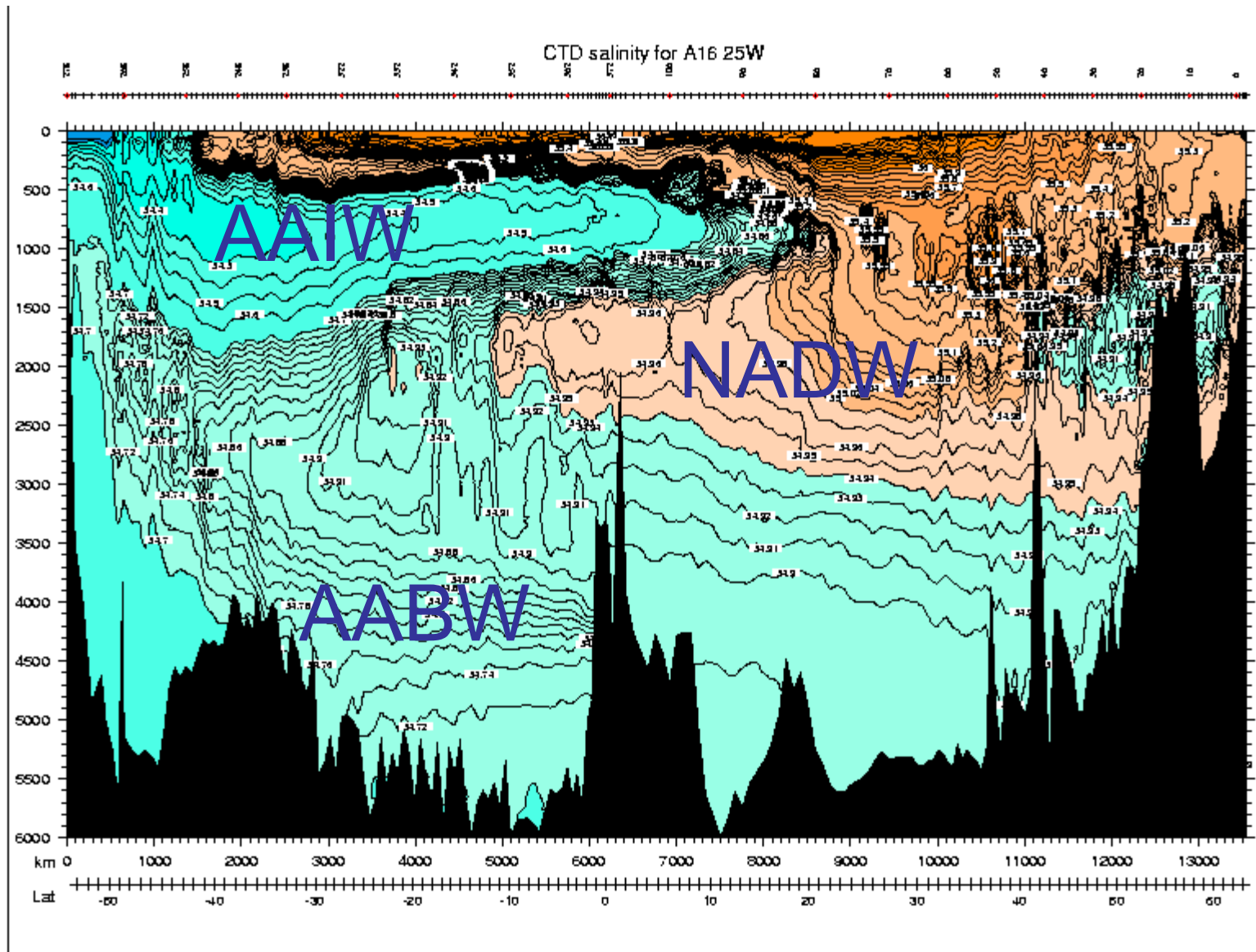
Ocean Dynamic Topography (cm) Oct 3-12, 1992

■ No Valid Data

# Observed Salinity Section Along 25W showing NADW, AAIW and AABW



# Observed Salinity Section Along 25W showing NADW, AAIW and AABW

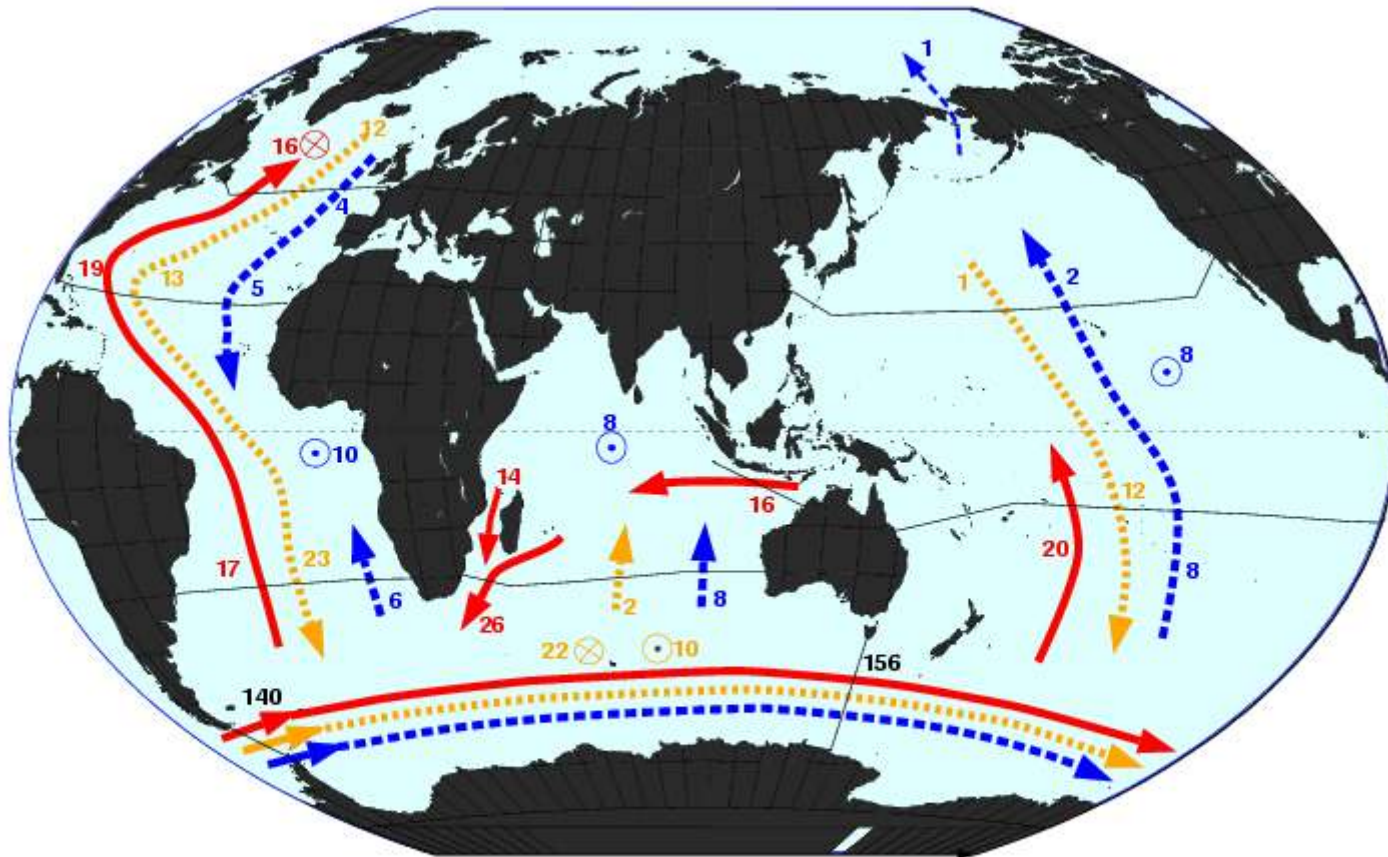


50S

EQ

50N

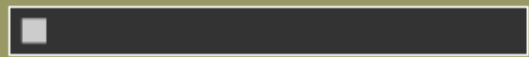
# Meridional Mass Transport Inferred from WOCE lines



shallow; intermediate; deep

—— WOCE line

(Talley)



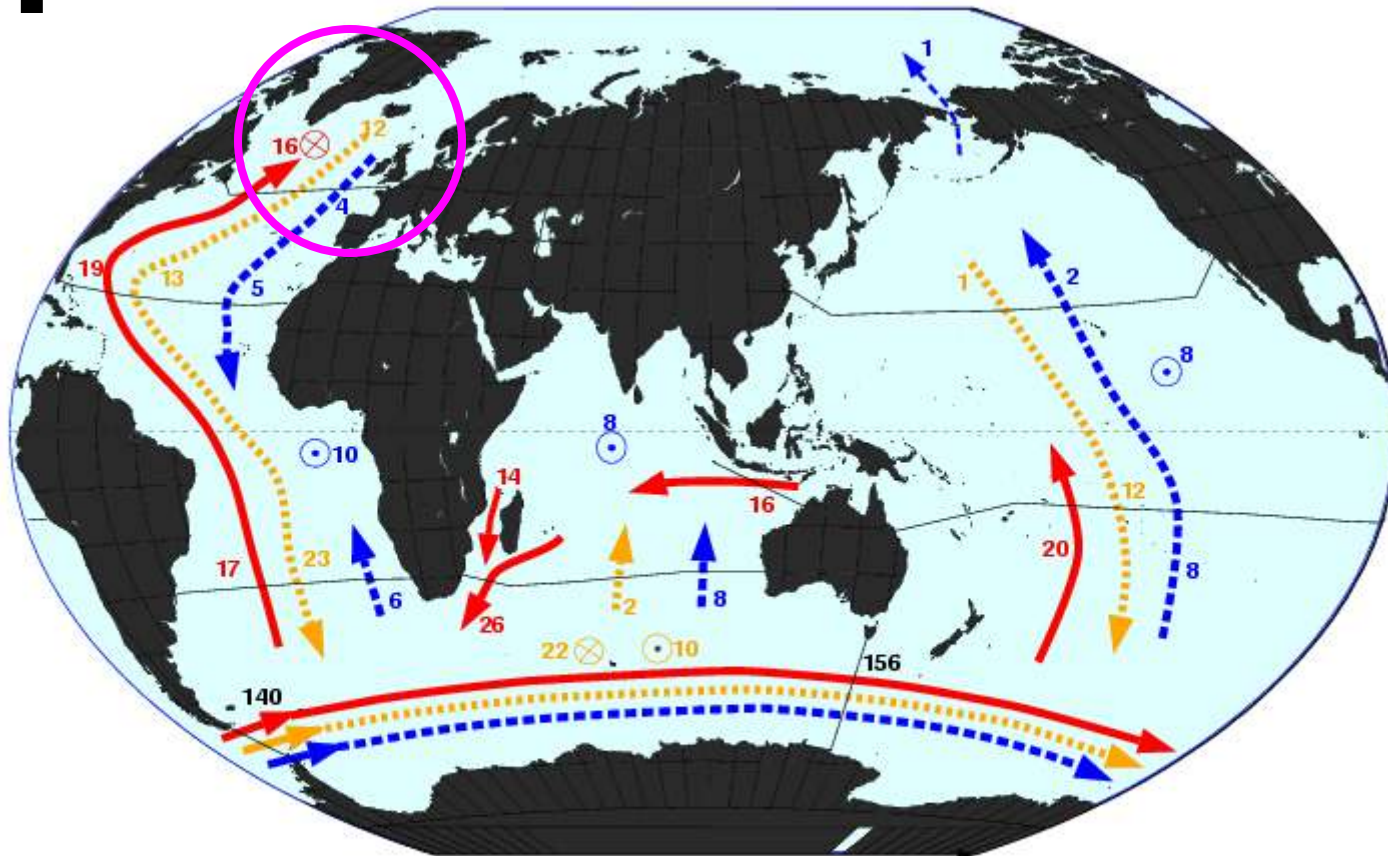
0 %

*Loading*



# Dansgaard-Oeschger events (MOC shutdowns)

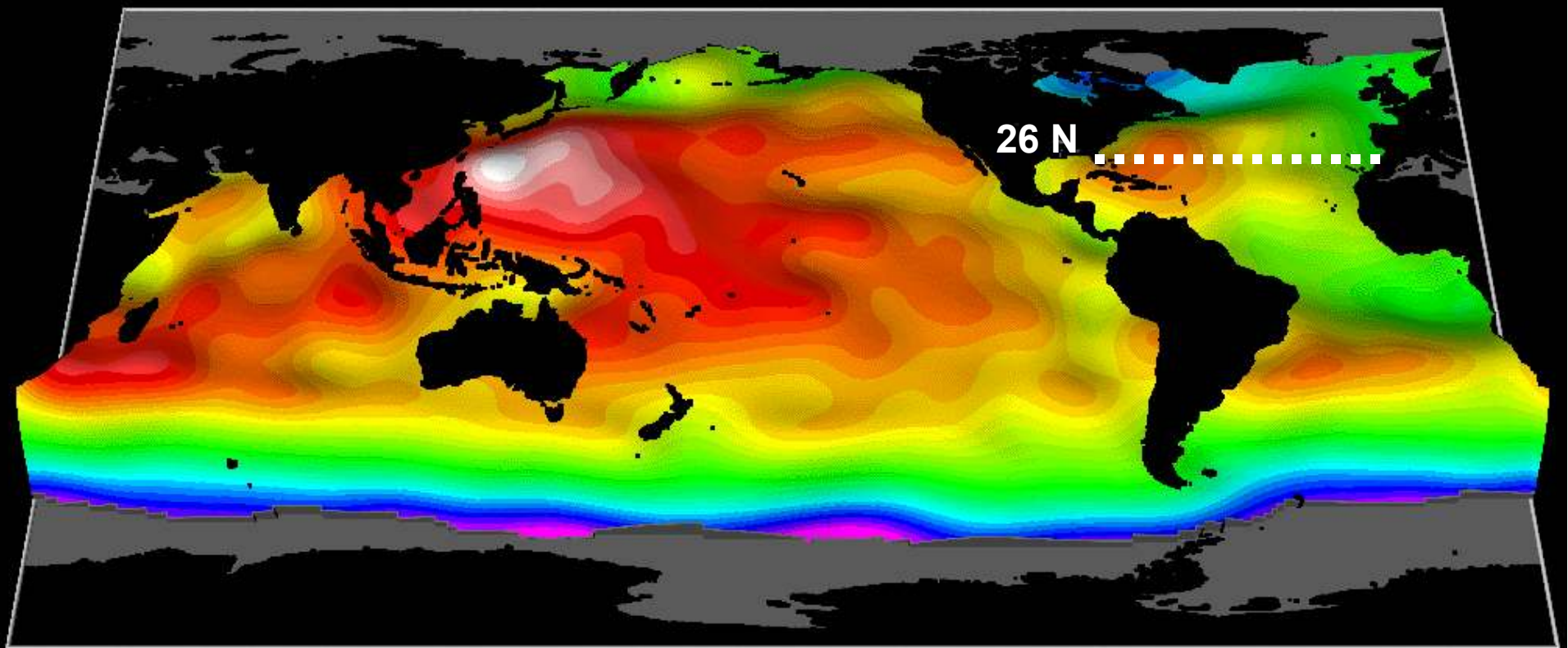
?



# **Estimated Decadal Changes in the North Atlantic Meridional Overturning Circulation and Heat Flux 1993-2004 (Wunsch & Heimbach, 2006)**

## Tools used :

- 4D-Var data assimilation
- Estimating the Circulation and Climate of the Ocean (ECCO)
- Model: MITgcm – global, 1 degree



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

# Estimated Decadal Changes in the North Atlantic Meridional Overturning Circulation and Heat Flux 1993-2004 (Wunsch & Heimbach, 2006)

11 yr assimilation,  
using all data,  
free run with adjusted  
surface fluxes

1 Sv =  $10^6 \text{ m}^3 \text{ s}^{-1}$

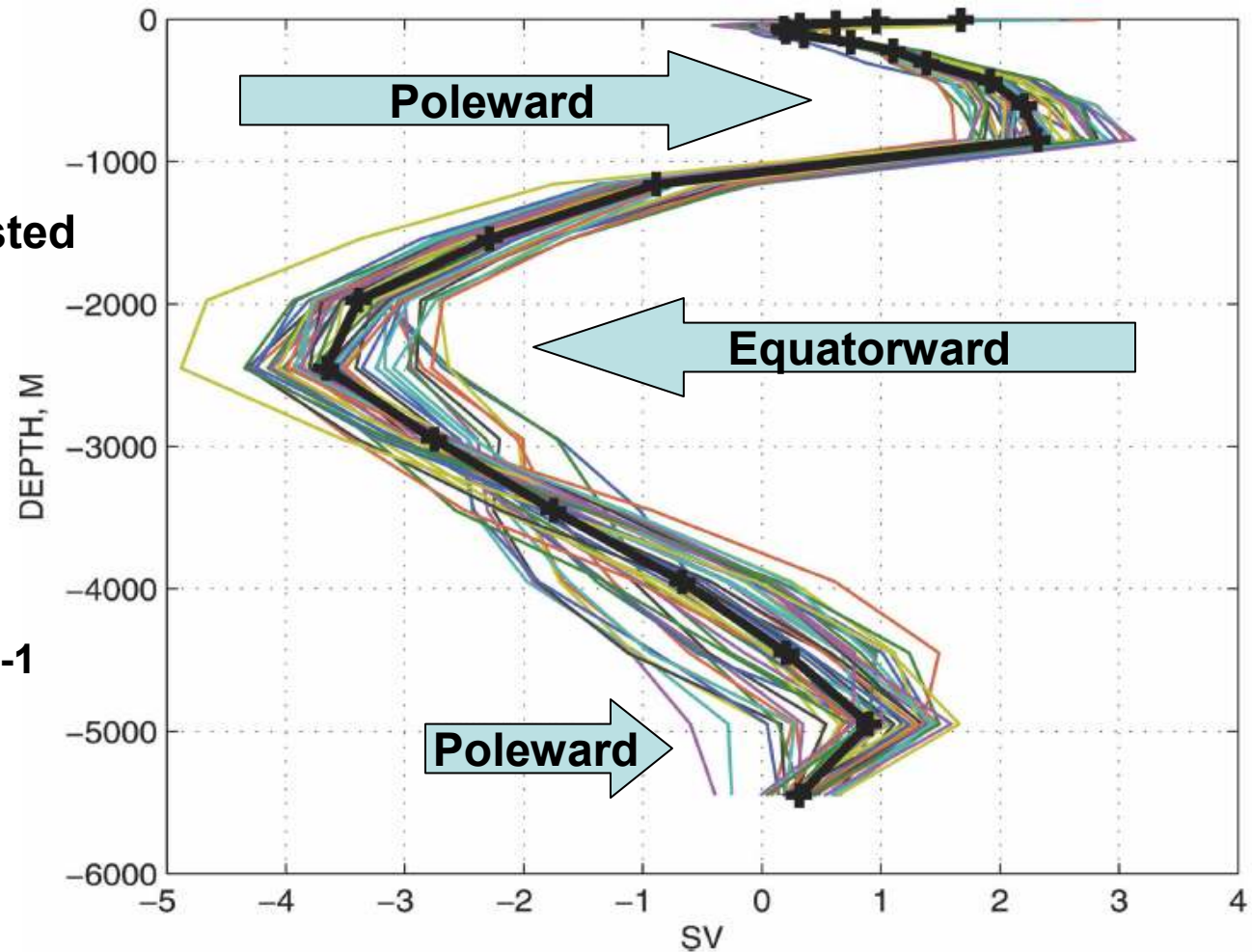


FIG. 3. Zonal integrals (Sv) of the North Atlantic seasonally averaged (3-month mean) velocity fields multiplied by the appropriate layer thickness as a function of depth. There is a near-zero value close to 1165-m depth. Plus signs and heavy line denote the time-mean values.



# Estimated Decadal Changes in the North Atlantic Meridional Overturning Circulation and Heat Flux 1993-2004 (Wunsch & Heimbach, 2006)

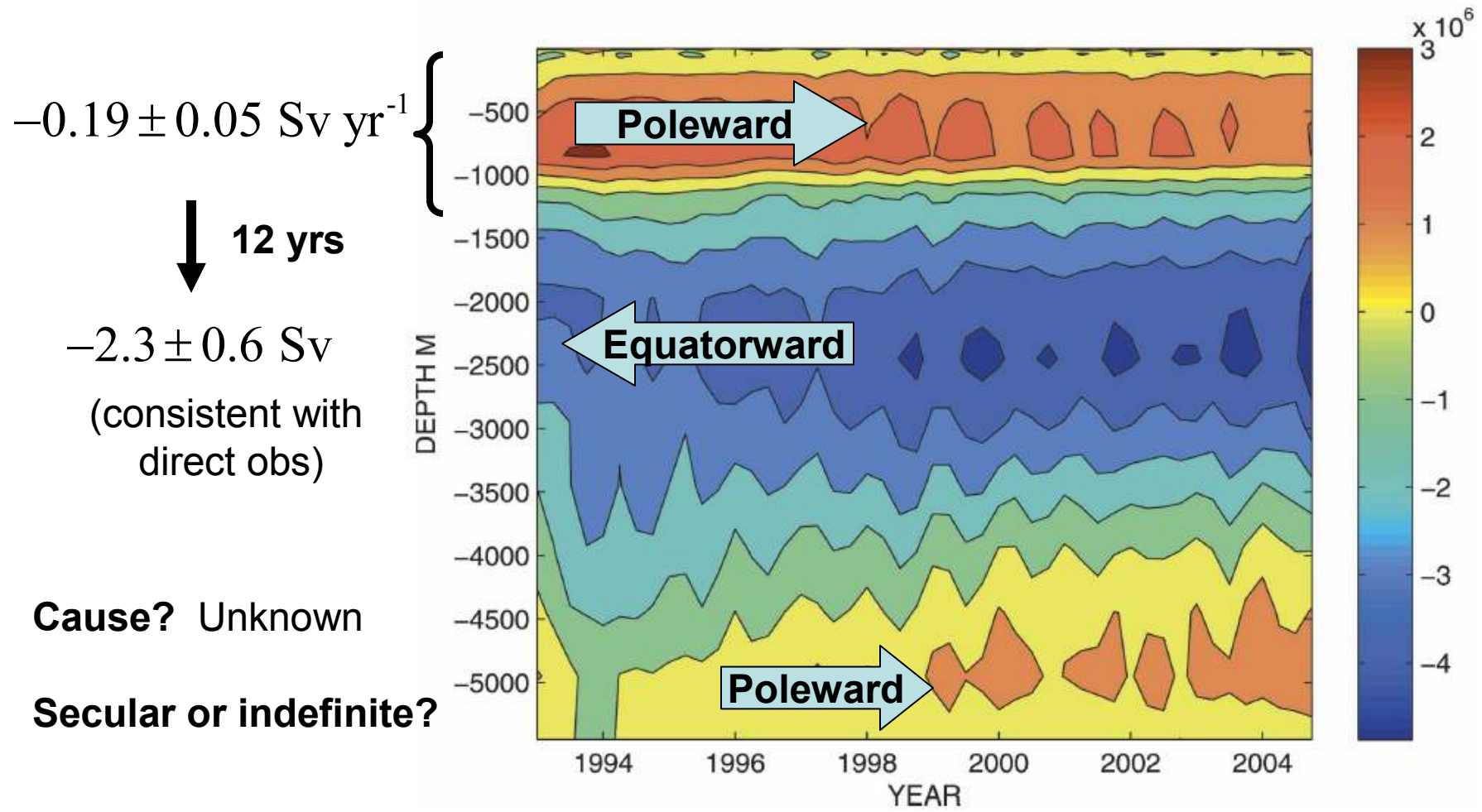


FIG. 9. Seasonal averages (3 months) of volume transport contours ( $\text{m}^3 \text{s}^{-1}$ ) through time as a function of depth (another rendering of the profiles in Fig. 3).



# Sensitivity of MOC to Surface Forcing

- Dansgaard-Oeschger events (MOC slow-downs)

- 0D models: Tziperman & Ioannou (2002)
- 2D models: Alexander & Monahan (2009)
- 3D idealized: Sévellec et al (2009); Zanna et al (2009)



**Singular vectors**



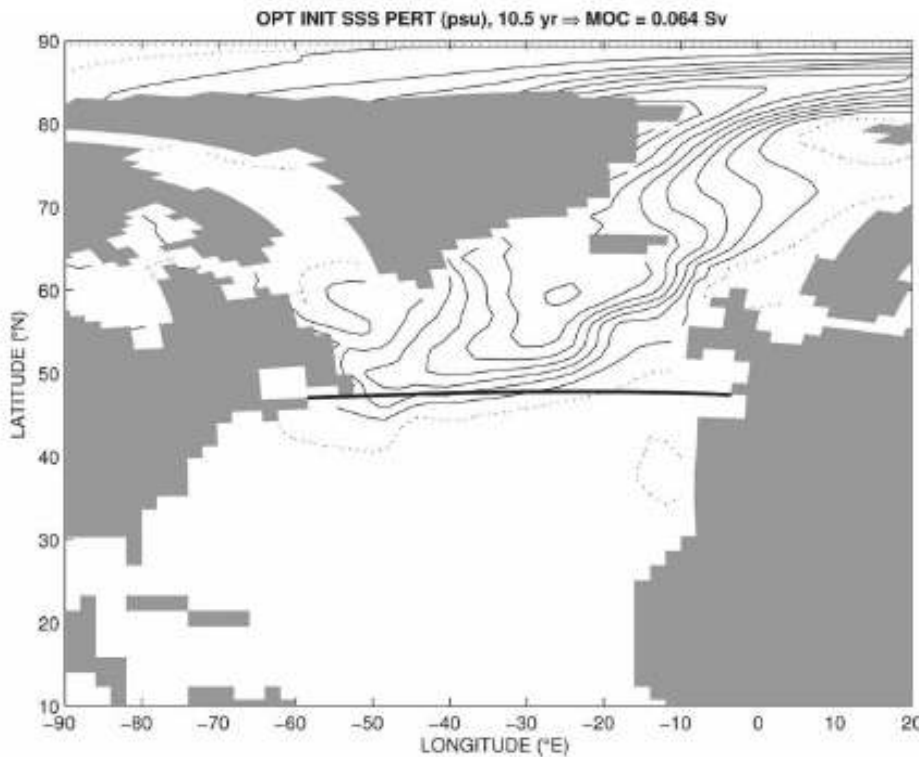
**Nonnormal dynamics associated with horizontal and vertical advection**

**Optimal Surface Salinity Perturbations of the  
Meridional Overturning and Heat Transport in  
a Global Ocean General Circulation Model  
(Sévellec et al, 2008)**

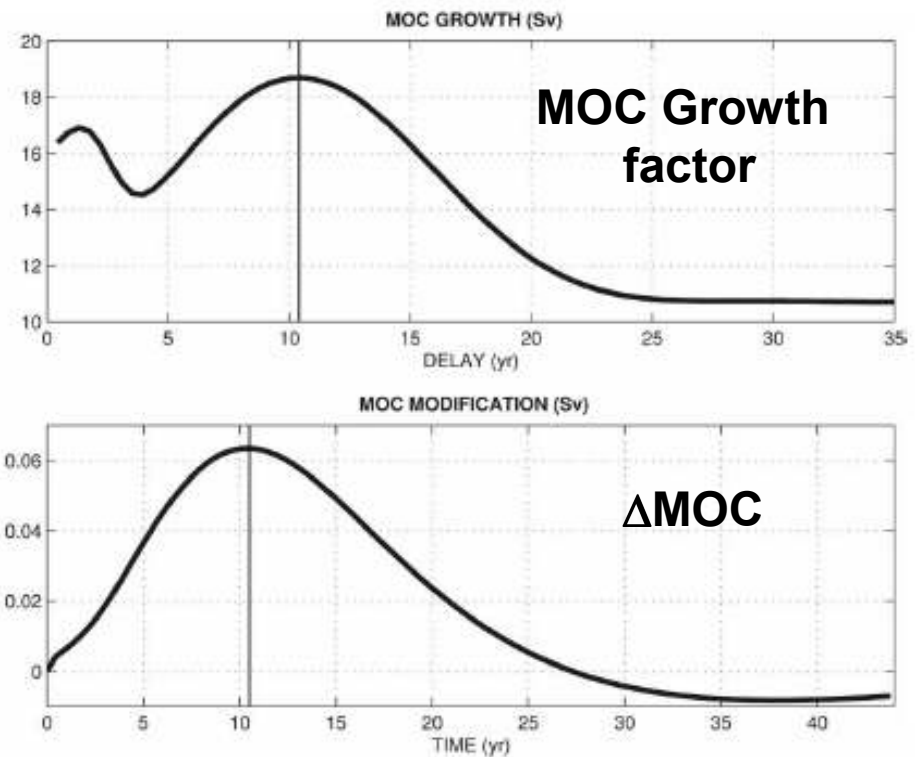
Tools used :

- Adjoint sensitivity analysis
- Model: OPA – global 2 degree

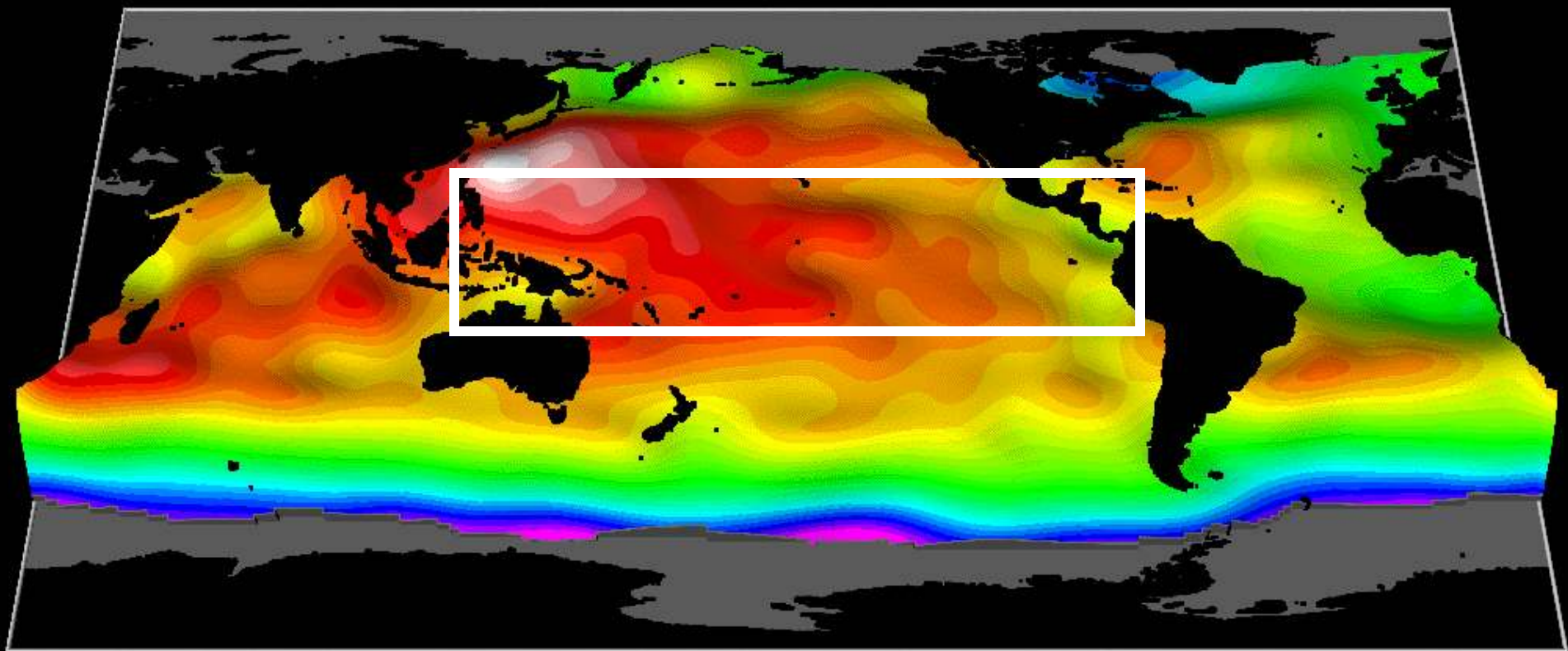
# Optimal Surface Salinity Perturbations of the Meridional Overturning and Heat Transport in a Global Ocean General Circulation Model (Sévellec et al, 2008)



Optimal SSS Perturbation  
(scaled to 1 psu amp.)



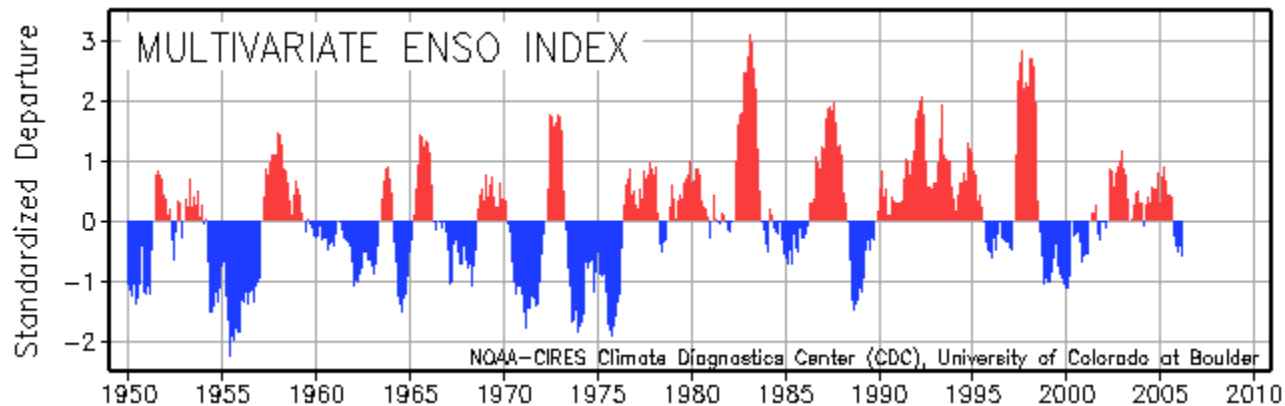
Upper bounds based on GSA:  
~0.8 Sv (11% of mean)  
~0.03 Pw (5% of mean)



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

# ENSO Irregularity



- The irregular nature of ENSO necessitates arguments related to nonlinearity or stochastic forcing.
- Most current theories of ENSO fall into two categories:
  - (1) nonlinear
  - (2) linear stochastically forced

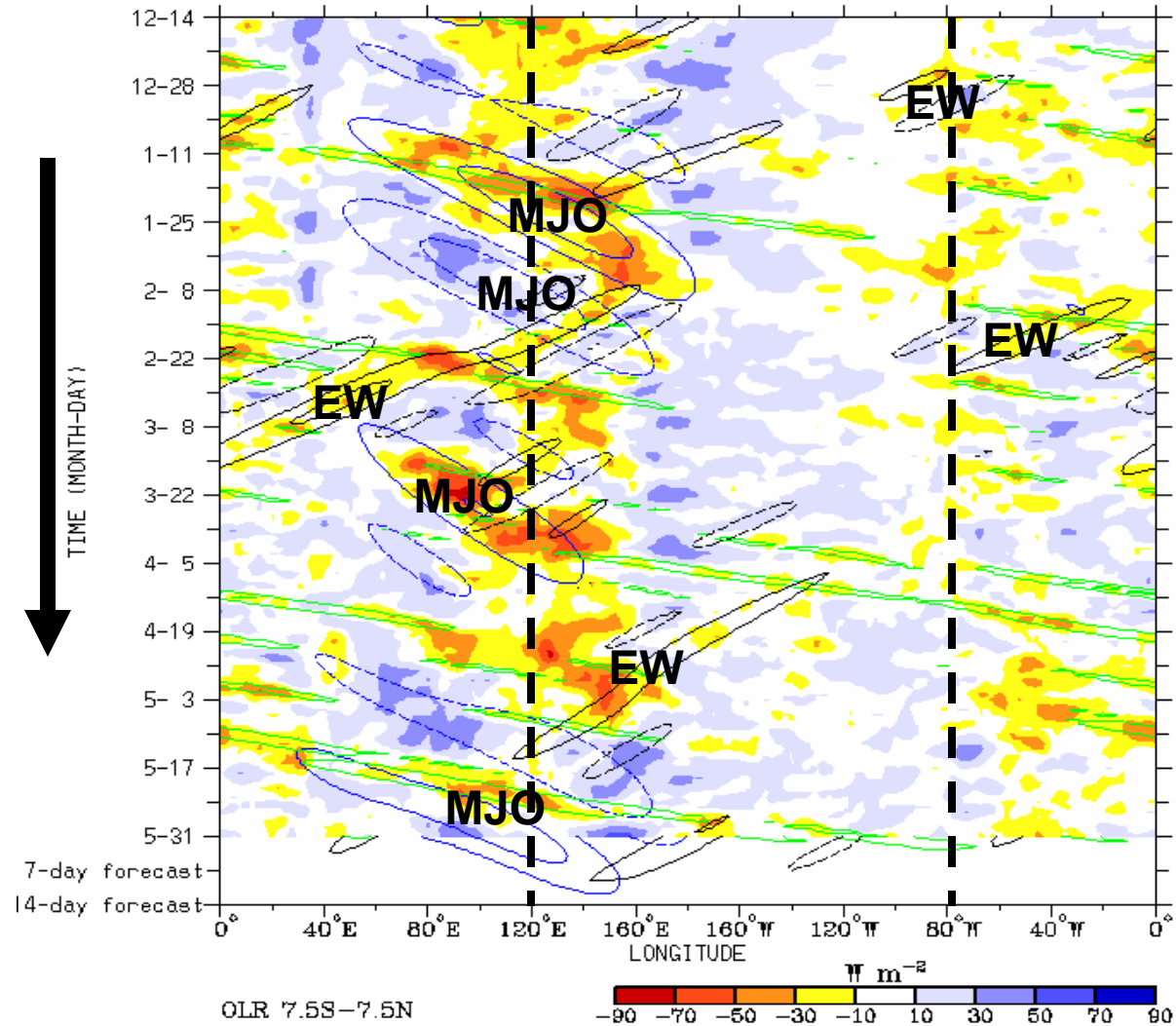


# Tropical Stochastic Forcing

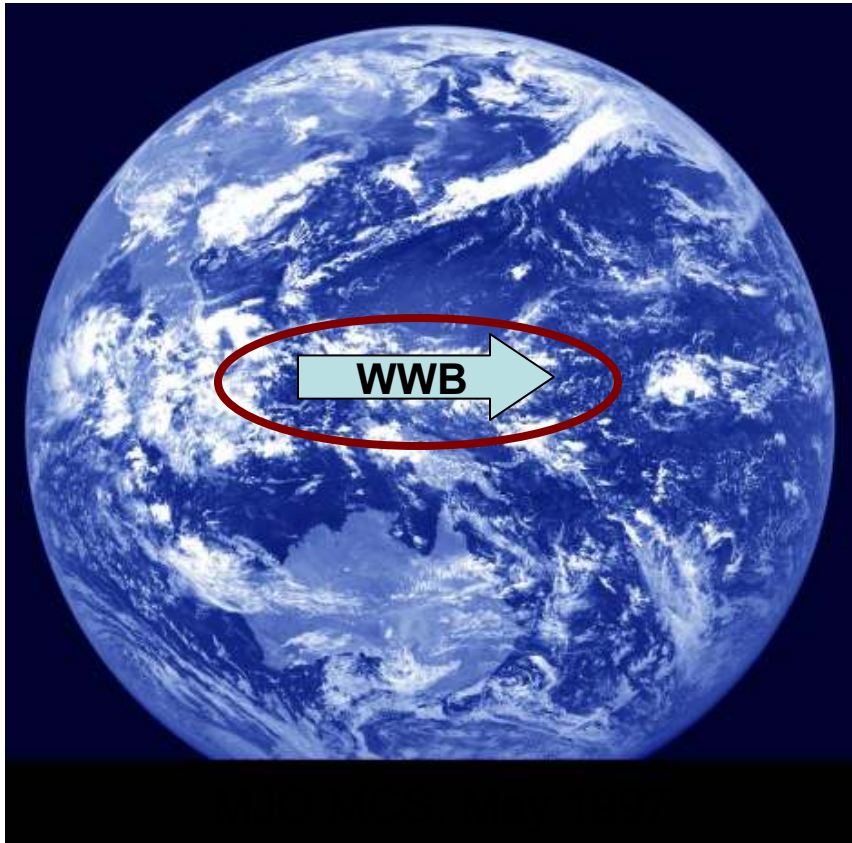
Real-time filtering superimposed upon 3drm OLR Anomalies  
MJO blue CINT 10, ER1 black CINT 10, Kelvin green CINT 15  
Negative contours solid, positive dashed (exl Kelvin)  
2005-12-14 to 2006- 5-31

MJO = Madden-Julian Oscillation

EW=Easterly Wave



# An Important Question

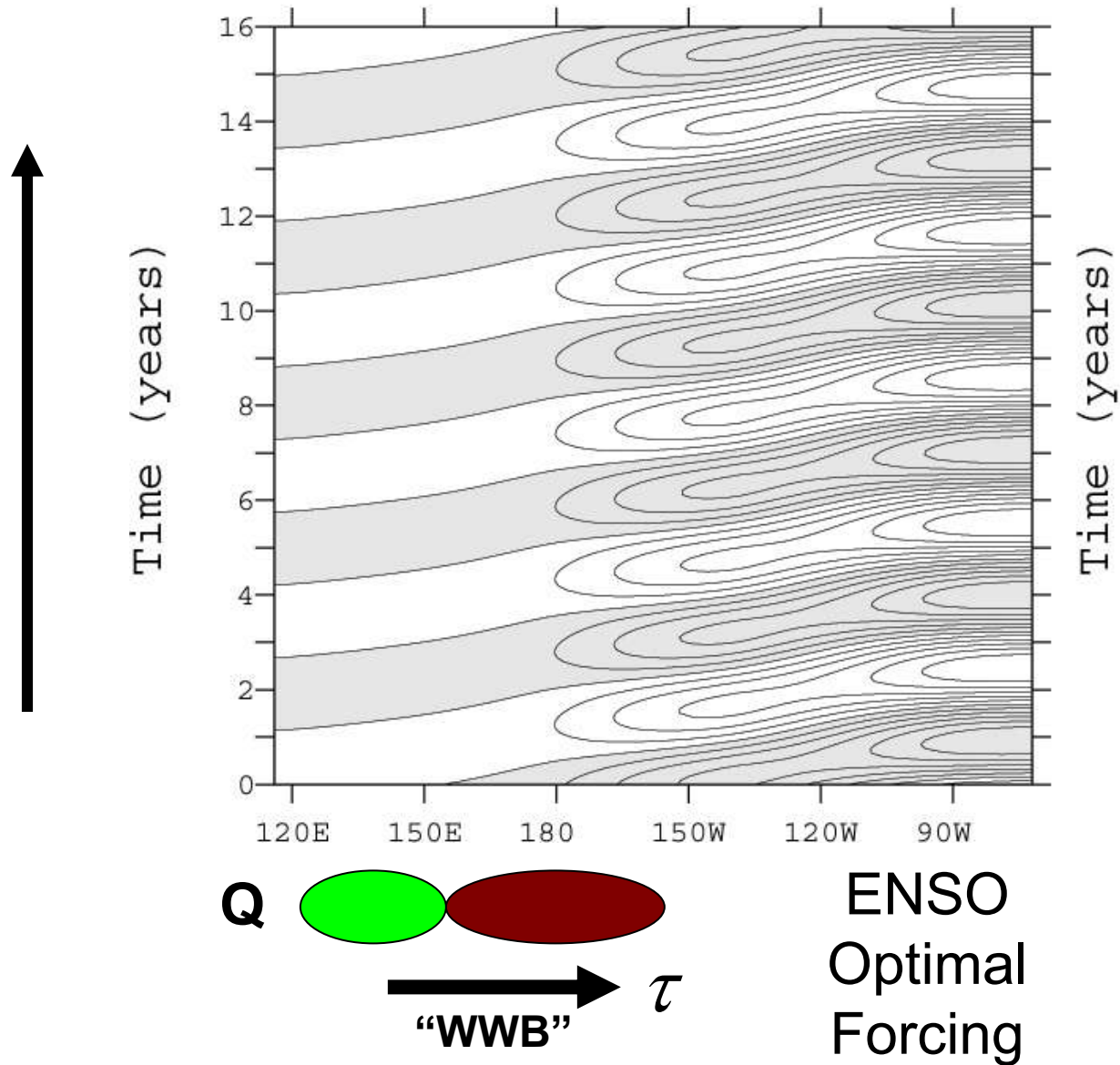


- Are the spatial and temporal characteristics of forcing important, or will any old forcing do the trick?
- In other words, are some forcings more efficient than others for exciting ENSO?
- The answer depends on the *nonnormality* of the dynamics.

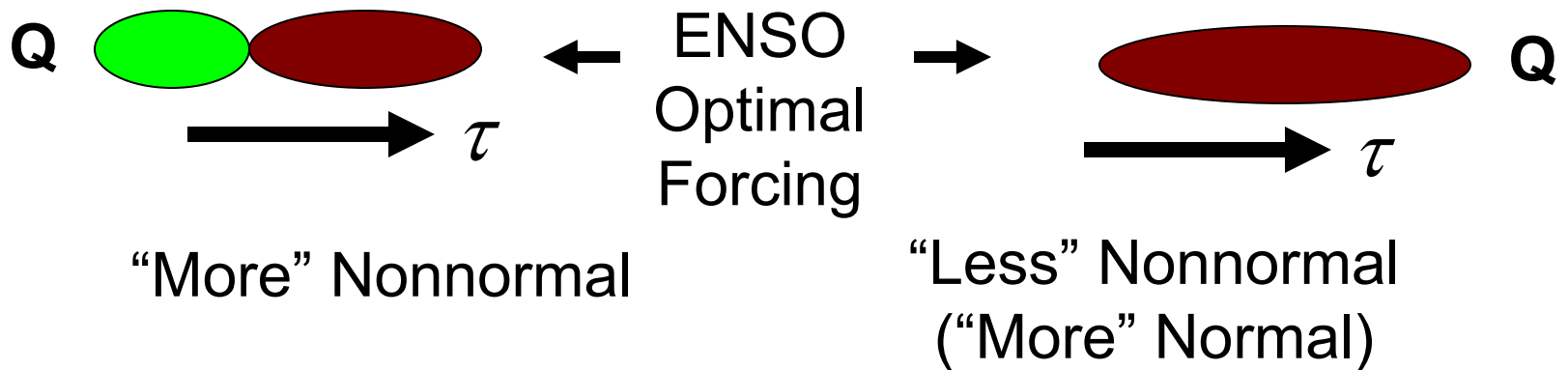
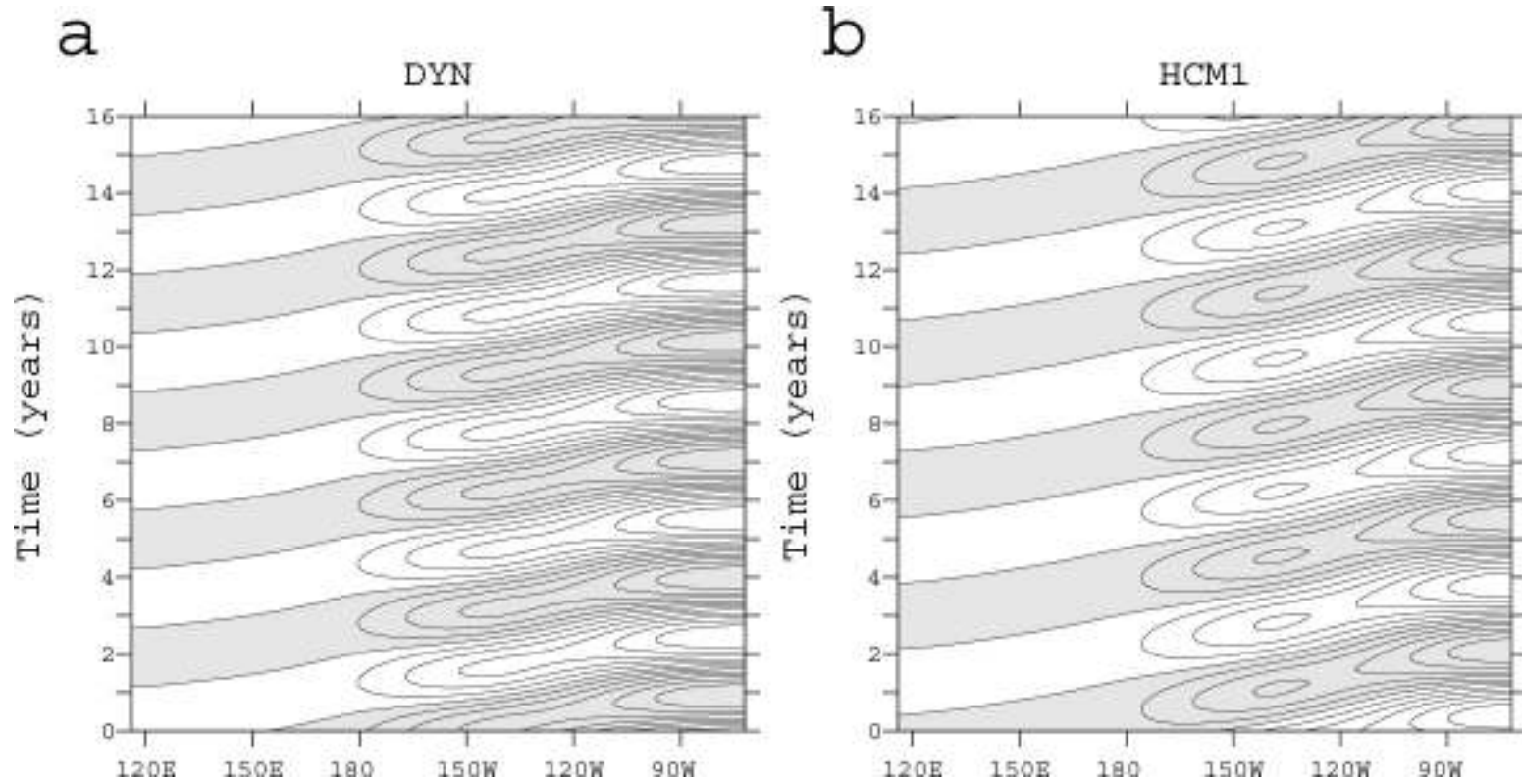
# Tools Used

- Singular value decomposition & pseudospectra
- Models: intermediate & hybrid coupled models

# Optimal Stochastic Forcing

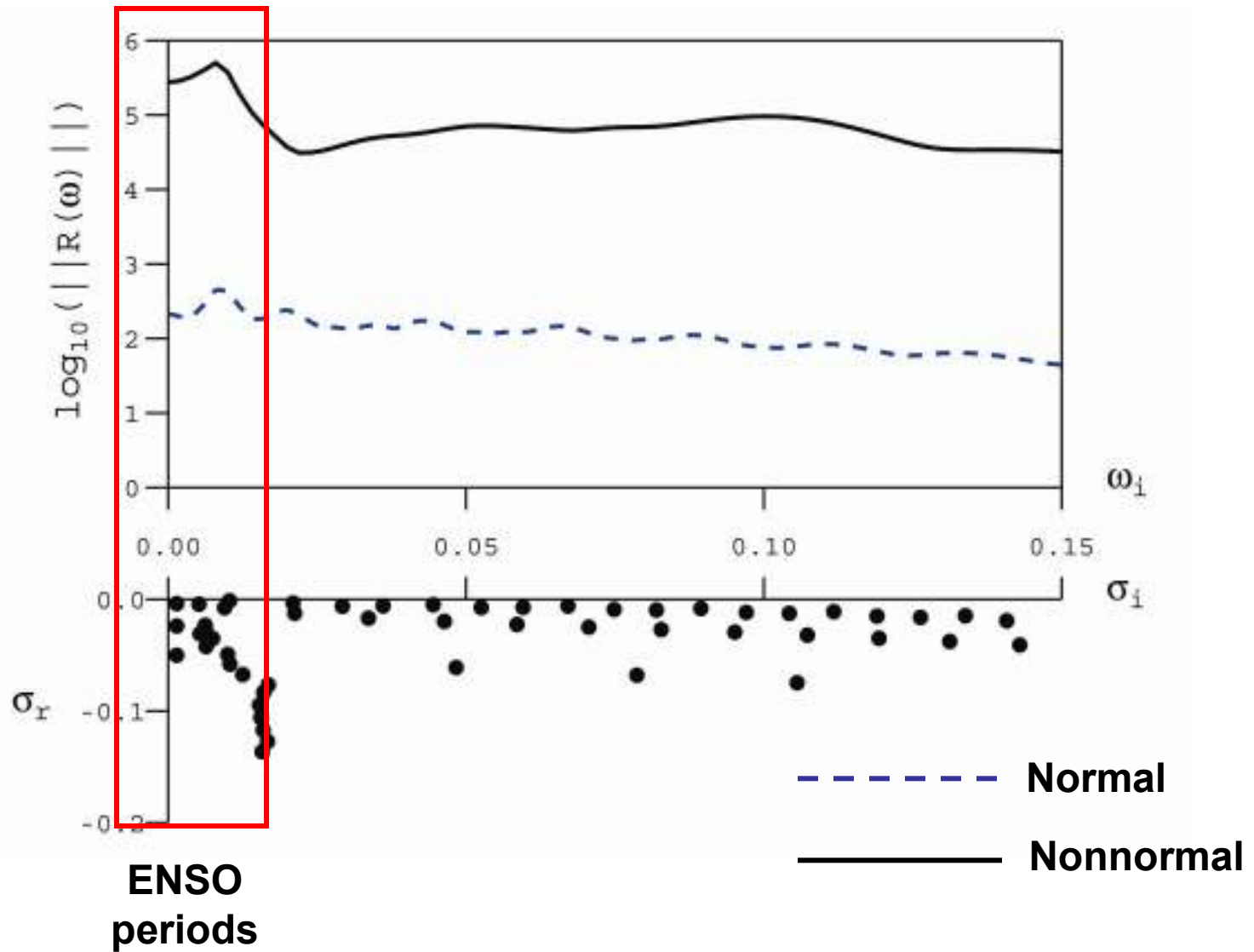


# Optimal Stochastic Forcing



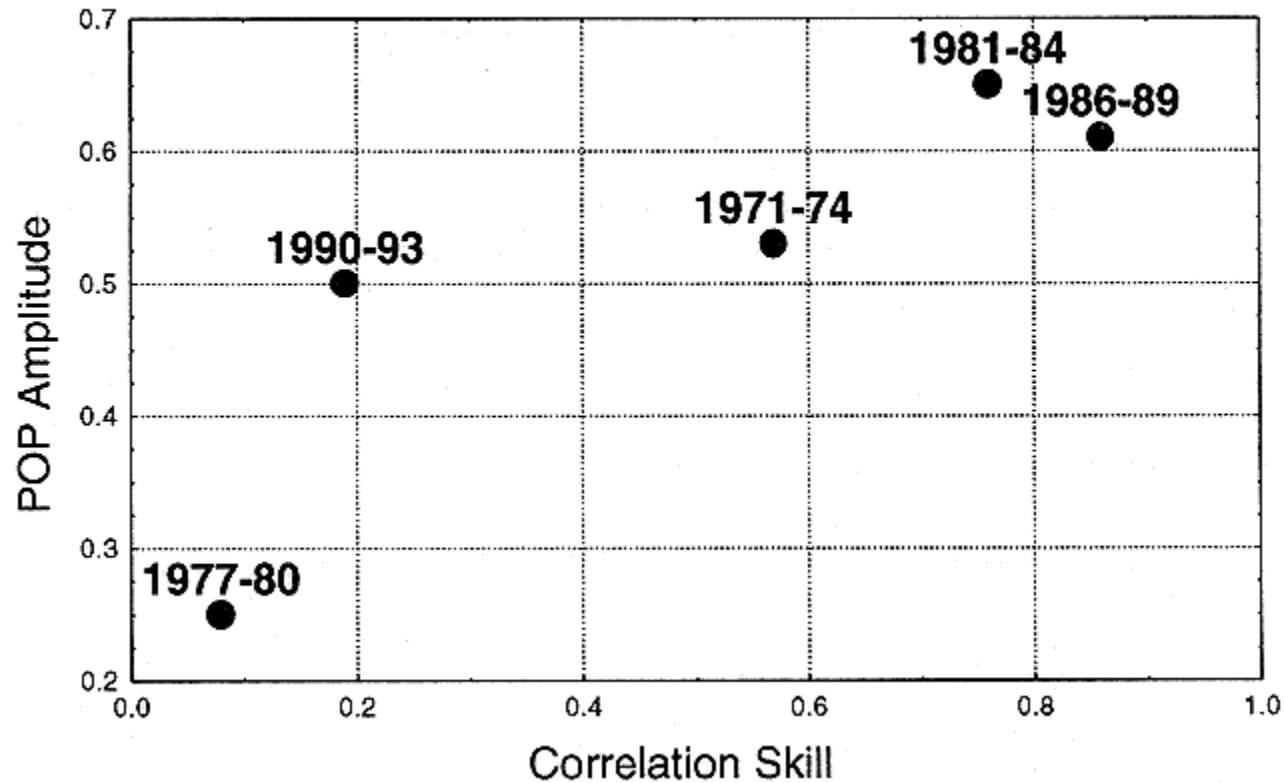


# Pseudoresonance

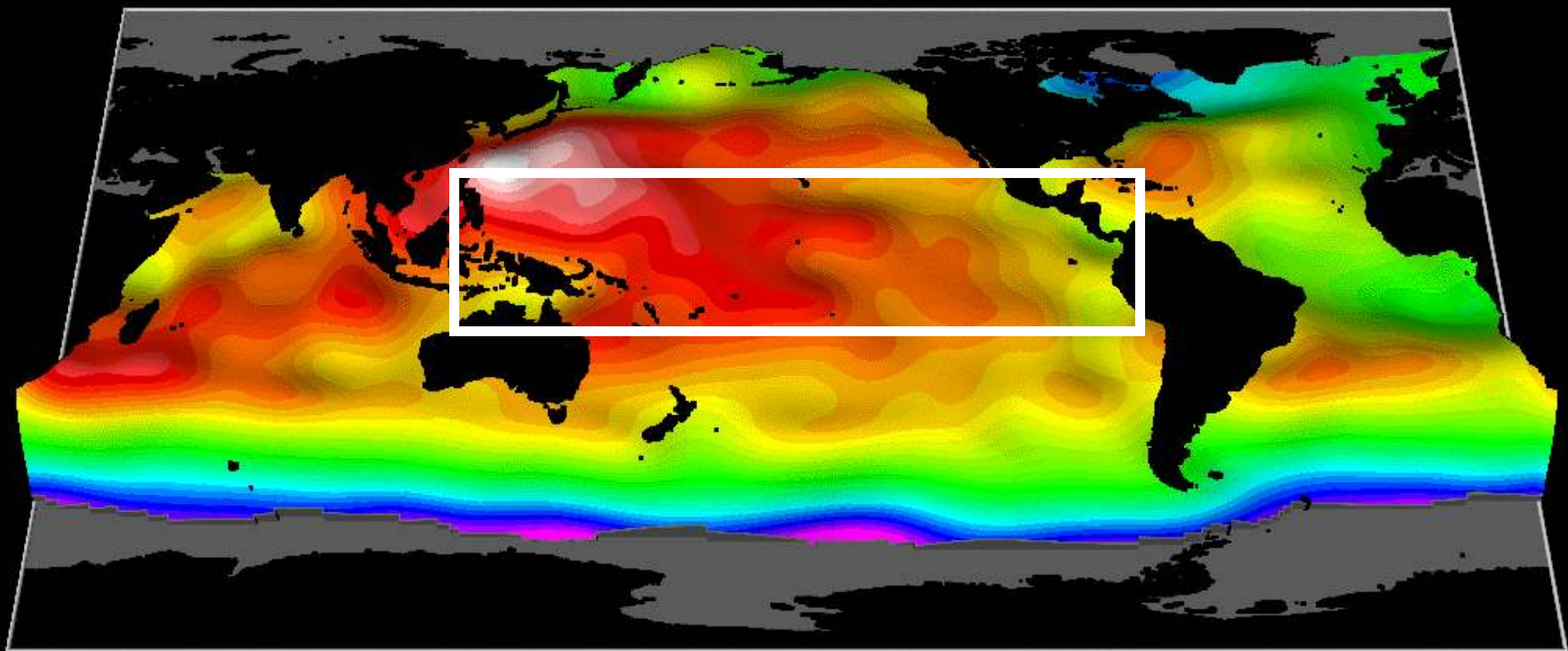


# Predictability

Plot of skill versus POP amplitude for various time periods



ENSO hindcast skill is proportional to ENSO amplitude



■ No Valid Data

Ocean Dynamic Topography (cm) Oct 3-12, 1992

# **A Midlatitude-ENSO Teleconnection Mechanism via Baroclinically Unstable Long Rossby Waves (Galanti & Tziperman, 2003)**

## Tools used :

- Adjoint sensitivity analysis
- Model: MOM, Pacific, 1-3 degrees

# A Midlatitude-ENSO Teleconnection Mechanism via Baroclinically Unstable Long Rossby Waves (Galanti & Tziperman, 2003)

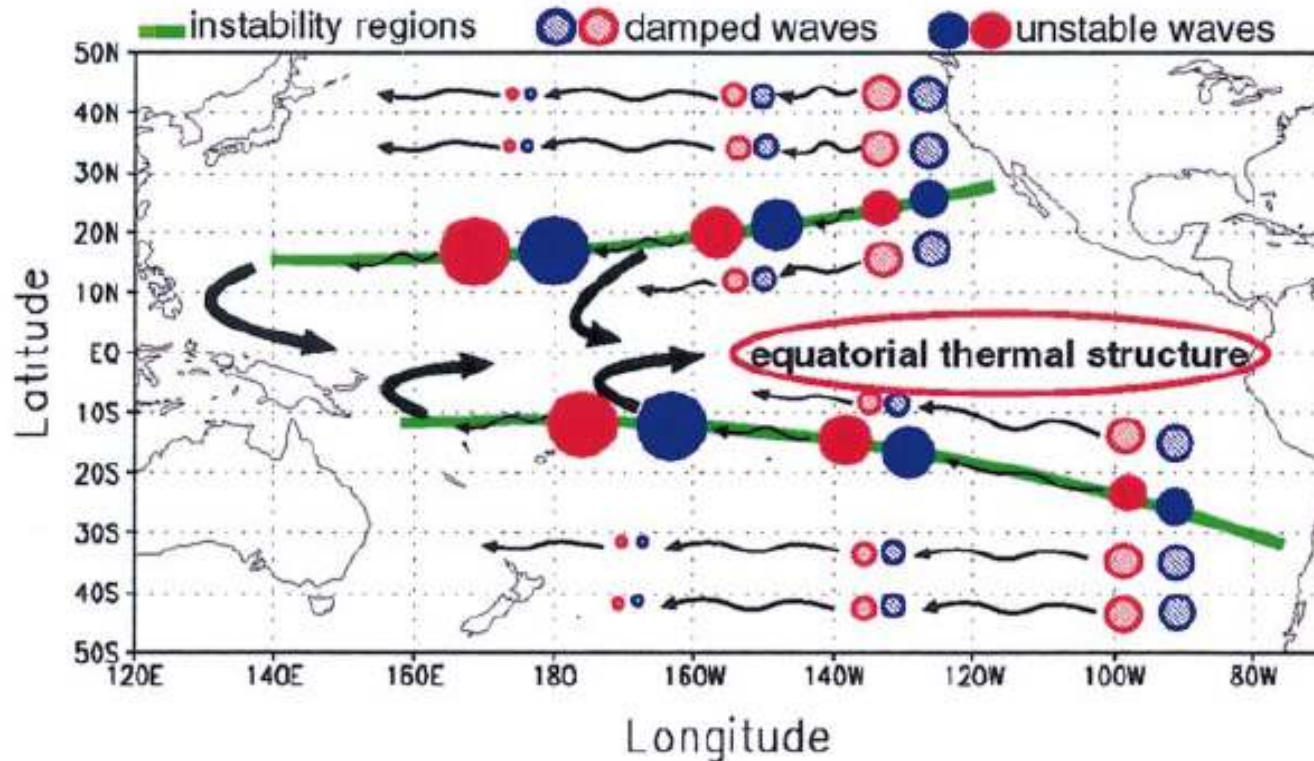


FIG. 1. A schematic figure of the mechanism proposed in this paper for a wave teleconnection from the midlatitude Pacific to the equator. Midlatitude planetary Rossby waves travel westward at all latitudes and are damped. The waves that are amplified in baroclinically unstable regions of the subtropical gyre arrive to the equator with a larger amplitude and therefore dominate the midlatitude signal there.



**We really have learned a lot of “cool” things  
about the ocean using adjoint models!**